

Mathematics Paper 2 23rd November 2017 FORM 4

Examiner	A Gunning	Moderator	C Mundy
Time	3 hours	Marks	150

PLEASE READ THE FOLLOWING INSTRUCTIONS CAREFULLY BEFORE ANSWERING THE QUESTIONS.

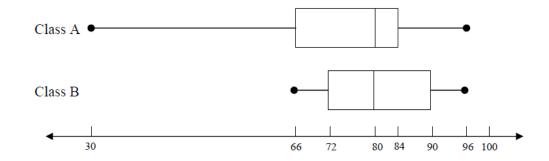
- This question paper consists of 21 printed pages. Please check that your question paper is complete. (The last pages have been left blank deliberately.)
- You have also been given an information sheet.
- All answers are to be written in this booklet.
- Read and answer all questions carefully.
- Number your answers exactly as the questions are numbered.
- It is in your own interest to write legibly and to present your work neatly.
- All necessary working, which you have used in determining your answers, must be clearly shown.
- Approved non-programmable calculators may be used except where otherwise stated. Where necessary give answers correct to 2 decimal places.
- Diagrams have not necessarily been drawn to scale.

Ques No	1	2	3	4	5	6	7	8	9	10	11	12	Total	%
Out of	17	10	16	13	32	10	13	5	10	6	5	13	150	
Mark														

QUESTION 1-a calculator may be used in this question.

43	70	55	60	85	92	65	62	75	58
(i)	Calo	culate tl	he mean	ı test m	ark.				
(ii)	Cald	culate tl	he stand						
(11)	Cur								
(iii)		v many mean?	grade 1	2 stude	ents obta	ained m	arks wit	thin one	standard deviation fro
(iii)			grade 1	2 stude	ents obta	ained m	arks wit	thin one	standard deviation fro
(iii)			grade 1	2 stude					standard deviation fro

(b) The box and whisker plots below summarise the final test scores for two of Mrs Smith's Mathematics classes from Grade 11.



_	(2)

(ii) Calculate the range for Class A.

				(1)

(iii) Calculate the inter quartile range for Class B?

_	
_	(1)

(iv) Comment on the distribution of the data set for Class A.

_		(1)	
-	·		

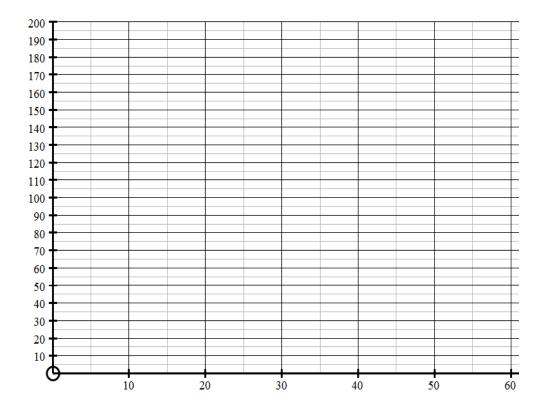
(c) The speed in km/hr of 170 snow skiers passing a certain point on a ski slope was recorded and summarised in the table below.

SPEED	FREQUENCY	CUMULATIVE FREQUENCY
$0 \le x < 10$	10	
$10 \le x < 20$	20	
$20 \le x < 30$	45	
$30 \le x < 40$	71	
$40 \le x < 50$	24	

(i) Complete the table above.

(2)

(ii) Draw an ogive curve of the cumulative frequency vs speed of skiers.



(4)

(iii) From your graph, determine the value of the median. Show clearly on your graph where this answer was obtained.

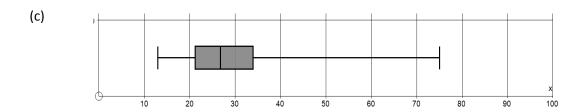
(1)

(iv) Use your graph to estimate the number of skiers that passed the point with speed greater than 35.

(1)

[17]

(a)		higher the range of a set of data, the higher the standard
	claim. Justify fully.	ollowing pair of data sets prove or disapprove the learner's
	Data set 1: 60; 80. 80. 80, 80, 10	00
	Data set 1: 00, 80: 80: 80; 80; 10 Data set 2: 62; 62; 62; 98; 98; 98	
(b)	Let a, b, c and d be integers such that	at $a < b < c$ and $c = d$.
	The mode of these four numbers is	11.
	The range of these four numbers is	8.
	The mean of these four numbers is	8.
	Calculate the values of a, b, c and d	(4)



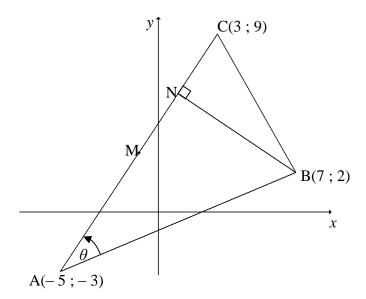
The above diagram represents the age demographics of Facebook users in South Africa.

Use this diagram to answer the following questions:

State whether the statement is true or false. If false, correct the statement.

he median age is between 2	25 and 30.	
0% of the users are over 34	•	

[10]



(a)	Calculate the length of AC. (Leave your answer in surd form.)	(3)
_		
_		
_		
_		

(b)	Determine the coordinates of M, the m	nidpoint of AC. (2	()

(c)	Calculate the gradient of AC.		

(d)	Hence, determine the equation of BN.	(3)
_		

e) Calculate the area of $\triangle ABC$ if N is the point (1; 6).	(3)
f) Calculate θ , correct to 1 decimal place.	(3)
DUESTION 4	[10
5 A	
3	
2	
5 -4 -3 -2 -1 1 2 3 4 5 X	
В	
å c	
L(1;5), $B(-3;-1)$ and $C(0;-3)$ are the vertices of a triangle.	
	(2)
a) Write down the coordinates of D if ABCD is a parallelogram.	(2)

b) Show that ABCD is in fact a rectangle.	(3)
e) If A, B and $E(5; y)$ are three collinear points, find the value of y.	(3)
(d) If the distance between C and $F(8; p)$ is 10 units, find the possible values of p .	(5)

SHOW ALL RELEVANT WORKING STEPS.

		$\frac{80^{\circ} + x}{100^{\circ} + x} \tan(-x - \frac{1}{200^{\circ} + x})$	100)
	COS(S	$90^{\circ} + x$)	
Prove t	hat 1	- + ¹ =	$=\frac{2}{\cos^2(180^\circ-x)}$
10101	$1+\sin x$	x 1-sin x	$\cos^2(180^\circ - x)$
For wh	ich values of	f x in the interval	al $0^{\circ} \le x \le 360^{\circ}$ is the identity in Question 5(b) undefined?

	Using a sketch, drawn in the relevant quadrant, given that $13 \sin x + 5 = 0$
	and $x \in [90^\circ; 270^\circ]$, without using a calculator, find the value of each of the following:
	$(i) \sin(90^{\circ} - x)$
	(ii) $tan(180^{\circ} - x)$
) S c	blve for x in each of the following
(i)	
(ii	$(\cos x - 2) (3\sin 2x - 2) = 0 \text{ giving a general solution.}$
_	

(2)

(f) Given that $\sin 34^{\circ} = t$, write each of the following in terms of t.

(i)	sin 214°			



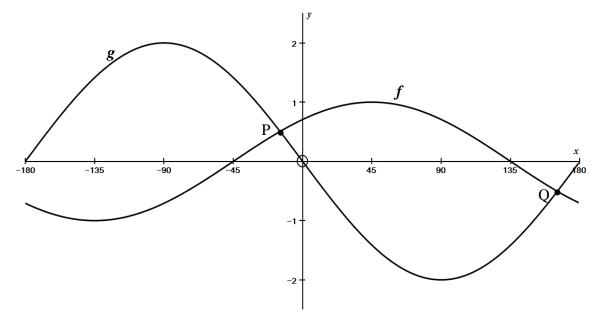
 $(iii) tan(-34^{\circ})$ (2)

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QUESTION 6

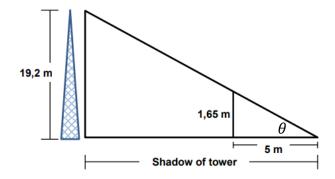
The sketch graph below shows the curves of f and g, defined by:

 $f(x) = \cos(x+b)$ and $g(x) = c \sin x$ where $x \in [-180^{\circ}; 180^{\circ}]$



If P(d	(0,51) and Q(165,36°; e) are the points of intersection of the two graphs, write down the
values	s of d and e .
For v (i)	which values of x is: $f(x) > 0$
(ii)	f(x).g(x) > 0
, ,	
If the	e y-axis is shifted 60° to the right, what will the new equation of f be?

(a) At a particular time during the day, a tower of height 19,2 m casts a shadow. At the same time, a person who is 1,65 m tall casts a shadow which is 5 m long.

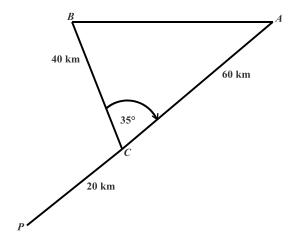


(i)	Calculate the value of θ .	(2)
111	Calculate the value of 0.	(2)

(ii)	What is the length of the shadow cast by the tower at that time?	(4)

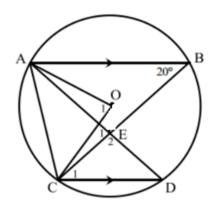
(b) A cyclist at training is on his way from *P* to *A*. When he reaches point *C*, the road forks. The road to the right leads directly to *A*, which is 60 km from *C*. *P* and *C* are 20 km apart. The road to the left leads to *A* via *B*. *C* and *B* are 40 km apart.

The angle between the roads (BC and AC), is 35° .



(i)	Calculate the difference between the distances of the two routes from <i>P</i> to <i>A</i> , correct to the			
	nearest kilometre.	(4)		
(ii)	Calculate \hat{B}	(3)		

In the diagram, O is the centre of the circle passing through A, B, D and C. AB // CD and $\hat{B} = 20^{\circ}$.

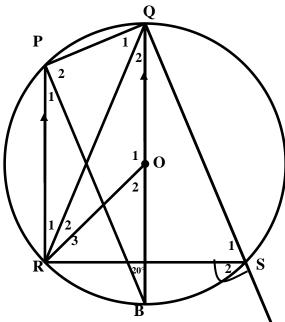


Complete the following statements and reasons to prove that AOEC is a cyclic quadrilateral. No extra steps or calculations can be added.

Statements	Reasons
$\hat{C}_1 = \dots$	Alt angles equal; AB //CD
$\hat{O}_1 = 40^{\circ}$	
$\widehat{D} = 20^{\circ}$	
$\hat{E}_1 = \dots$	Ext angle Δ
∴ AOEC is cyclic	

[5]

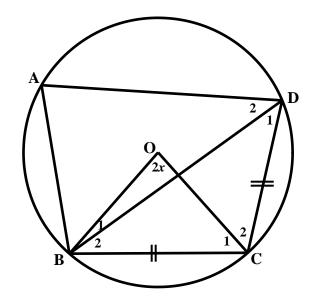
In the diagram below, O is the centre of the circle. PR is parallel to QB. QOB is a diameter. $\hat{PBQ}=20^{\circ}$



Find, with	h reasons, the sizes of the following ang	gles.	(2 marks each)
	Statement	Reason	
(i)	\hat{P}_2		
(ii)	\widehat{P}_1		
(iii)	\widehat{Q}_2		
(iv)	\hat{O}_2		
(v)	$\hat{\mathcal{S}}_2$		

[10]

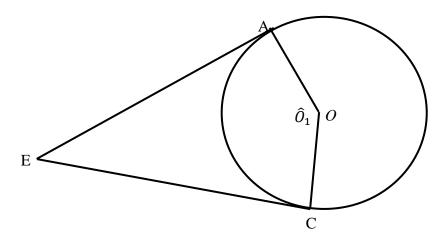
In the diagram alongside, the circle with centre O has BC = CD and $B\hat{O}C = 2x$.



Dete	rmine, with reasons, in terms of x .		Reasons
(i)	$\widehat{\mathcal{D}}_1$	(2)	
(ii)	BÂD	(4)	
			[6]

Refer to the sketch below.

In the diagram O is the centre of the circle with AE and CE tangents to the circle centre $O.\ \hat{O}_1=127^\circ$

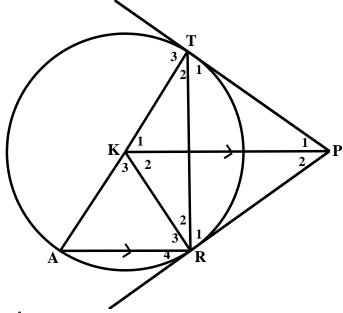


Calculate, with reasons, the size of \hat{E} .

(5)

STATEMENT	REASONS

In the figure below PT and PR are tangents to the circle at T and R respectively. Also PK II RA. $\hat{P}_1 = \hat{P}_2$. **Do not assume** that K is the centre of the circle.



(i)	Why is $\hat{R}_4 = \hat{P}_2$?	(1)

(ii)	Prove, with reasons, that KTPR is a cyclic quadrilateral.	(6)

Prove that PK bisects $T\hat{K}R$.	

[13]