

Grade 12

Mathematics P2-MEMO
September 2020

MARKS: 150
TIME: 3 hours

NOTE:

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed out version.
- Consistent accuracy applies in ALL aspects of the marking guidelines.
Stop marking at the second calculation error.
- Assuming answers/values in order to solve a problem is NOT acceptable.

NOTA:

- As 'n kandidaat 'n vraag TWEE KEER beantwoord, merk slegs die EERSTE poging.
- As 'n kandidaat 'n antwoord van 'n vraag doodtrek en nie oordoen nie, merk die doodgetrekte poging.
- Volgehoue akkuraatheid word in ALLE aspekte van die nasienriglyne toegepas.
Hou op nasien by die tweede berekeningsfout.
- Aanvaar van antwoorde/waardes om 'n probleem op te los, word NIE toegelaat nie.

GEOMETRY / MEETKUNDE:

| | |
|----------------|---|
| S | A mark for a correct statement (a statement mark is independent of a reason) |
| | <i>'n Punt vir 'n korrekte bewering.</i> (<i>'n Punt vir 'n bewering is onafhanklik van die rede.</i>) |
| R | A mark for a correct reason . (a reason mark may only be awarded if the statement is correct.) |
| | <i>'n Punt vir 'n korrekte rede.</i> (<i>'n Punt word slegs vir 'n rede toegeken as die bewering korrek is.</i>) |
| S&R | Award a mark if the statement AND reason are both correct. |
| | <i>Ken 'n punt toe as beide die bewering EN rede korrek is.</i> |

QUESTION/ VRAAG 1

| # | Suggested answer(s)/ Voorgestelde antwoord(e) | Descriptors/ Beskrywers | Mark/ Punt | | | | | | | | | | | | | | | | | | | | |
|--|--|---|------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|---|--|--|--|--|--|--|--|--|--|
| <div style="border: 1px solid black; padding: 5px; display: inline-block;"> Recover/ Herstel </div> | | | | | | | | | | | | | | | | | | | | | | | |
| <table border="1" style="margin: auto;"> <tr> <td>8</td> <td>39</td> <td>63</td> <td>69</td> <td>104</td> <td>141</td> <td>183</td> <td>191</td> <td>301</td> <td>592</td> </tr> <tr> <td colspan="10" style="text-align: center;">Source/ Bron: https://www.worldometers.info/coronavirus/?utm_campaign=homeAdvegas1?#countries</td> </tr> </table> | | | | 8 | 39 | 63 | 69 | 104 | 141 | 183 | 191 | 301 | 592 | Source/ Bron: https://www.worldometers.info/coronavirus/?utm_campaign=homeAdvegas1?#countries | | | | | | | | | |
| 8 | 39 | 63 | 69 | 104 | 141 | 183 | 191 | 301 | 592 | | | | | | | | | | | | | | |
| Source/ Bron: https://www.worldometers.info/coronavirus/?utm_campaign=homeAdvegas1?#countries | | | | | | | | | | | | | | | | | | | | | | | |
| 1.1 | Standard deviation/ <i>Standaardafwyking</i> = 163,13 | ✓ ✓ Answer/Antwoord | (2) K | | | | | | | | | | | | | | | | | | | | |
| 1.2 | Mean/ <i>Gemiddelde</i> : 169,1 (5,97; 332.23) Thus/ <i>Dus</i> : 9 countries/ <i>Lande</i> | ✓ Mean/ <i>Gemiddelde</i> ✓ Boundaries/ <i>Eindpunte</i> ✓ Answer/Antwoord | (3) R | | | | | | | | | | | | | | | | | | | | |
| 1.3 | False ; The infection rate could have been higher./ Virus was probably detected earlier there/ <i>Vals; Die infeksiekoers kon hoër wees/ Virus was waarskynlik daar gevind</i> : True ; better medical facilities/ Earlier detection lead to earlier safety precautions, etc/ <i>Waar; Better fasiliteite; mediese fasiliteite/ Vroeër waarneming lei tot vroeër veiligheidsmaatreels, ens</i> | ✓ Selection/ <i>Keuse</i> ✓ Reason/ <i>Rede</i> <i>Reason must justify</i> TRUE/ FALSE 2 or 0 | (2) P | | | | | | | | | | | | | | | | | | | | |
| 1.4 | Sum/ <i>Som</i> : 1691 New mean/ <i>Nuwe gemidd</i> : $209.72 \times 11 = 2306.92$ $2306.92 - 1691 = 616$ cases/ <i>gevalle</i> | ✓ New Total/ <i>Nuwe Totaal</i> ✓ Answer/Antwoord | (2) C | | | | | | | | | | | | | | | | | | | | |
| | | | [9] | | | | | | | | | | | | | | | | | | | | |

QUESTION/ VRAAG 2

| # | Suggested answer(s)/ Voorgestelde antwoord(e) | Descriptors/ Beskrywers | Mark/ Punt | | | | | | | | | | | | | | | | | | |
|--|---|---|------------|------|-----|---|---|---|---|-------------------------------------|----|----|-----|-----|-----|---|--|--|--|--|--|
| <table border="1" style="margin: auto;"> <tr> <td>Week</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> </tr> <tr> <td>No of Deaths/ <i>Getal sterftes</i></td> <td>62</td> <td>69</td> <td>160</td> <td>236</td> <td>265</td> </tr> <tr> <td colspan="6" style="text-align: center;">Source/ Bron: https://www.worldometers.info/coronavirus/country/south-africa/</td> </tr> </table> | | | | Week | 1 | 2 | 3 | 4 | 5 | No of Deaths/ <i>Getal sterftes</i> | 62 | 69 | 160 | 236 | 265 | Source/ Bron: https://www.worldometers.info/coronavirus/country/south-africa/ | | | | | |
| Week | 1 | 2 | 3 | 4 | 5 | | | | | | | | | | | | | | | | |
| No of Deaths/ <i>Getal sterftes</i> | 62 | 69 | 160 | 236 | 265 | | | | | | | | | | | | | | | | |
| Source/ Bron: https://www.worldometers.info/coronavirus/country/south-africa/ | | | | | | | | | | | | | | | | | | | | | |
| 2.1 | <p style="text-align: center;">Covid-19 deaths/ sterftes (per week)</p> | ✓ Correct axes/ <i>Korrekte asse</i> ✓ Plotting of points/ <i>Afstip van punte</i> | (2) K | | | | | | | | | | | | | | | | | | |

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|-----|--|--|------|---|
| 2.2 | $A = -13,5; B = 57,3$ $y = -13,5 + 57,3x$ | ✓ A and/ en B ✓ equation/ vergelyking | (2) | R |
| 2.3 | Graph/ Grafiek | ✓ + gradient/ gradient; ✓ through/ deur ≈ 160 | (2) | K |
| 2.4 | $r = 0,97;$ Strong positive relation/ Sterk positiewe verwantskap | ✓ Value of/ Waarde van r; ✓ strong positive/ sterk positiewe | (2) | K |
| 2.5 | Humankind would be totally wiped out/ A cure would be found sooner or later/ People practice safety measures/ Mense sal dan totaal uitgewis wees/ 'n Entstof sal een of ander tyd gevind word/ mense pas veiligheidmaatreëls toe. | ✓ Answer/ Antwoord | (1) | P |
| 2.6 | $y = -13,5 + 57,3(12)$ ≈ 674 | ✓ Subst 12 in eq/ vervang 12 in vgl ✓ Answer/ Antwoord -1 if decimal is stated; | (2) | R |
| 2.7 | Reaching its peak by this week OR number of deaths increased drastically over the last few weeks OR the least squares regression model is just an estimation of this situation/ Bereik sy piek teen hierdie week OF aantal sterftes het drasties toegeneem tydens die vorige paar weke OF die kleinste-kwadrateregressiemodel is slegs 'n benadering van die situasie. | ✓ Valid reason/ Geldige rede | (1) | P |
| | | | [12] | |

QUESTION/ VRAAG 3

| # | Suggested answer(s)/ Voorgestelde antwoord(e) | Descriptors/ Beskrywers | Mark/ Punt | |
|-------|--|---|------------|---|
| 3.1.1 | $EF = \sqrt{(-2 - 4)^2 + (-1 - 2)^2}$ $= \sqrt{45} \quad [= 3\sqrt{5} = 6,71]$ | ✓ subst/ vervang in EF ✓ Answer/ Antwoord | (2) | K |
| 3.1.2 | $m_{DH} = \tan D\hat{H}O$ $= \tan 45^\circ$ $= 1$ | ✓ $m_{DH} = \tan 45^\circ$ AO = no marks/ geen punte | (1) | K |
| 3.1.3 | $m_{DE} = \frac{d - (-1)}{2 - (-2)} = 1$ $\frac{d + 1}{4} = 1$ $d + 1 = 4$ $\therefore d = 3$ | ✓ subst/ vervang m_{DE} ✓ simplify/ vereenvoudig AO = no marks/ geen punte | (2) | R |
| 3.1.4 | GF \parallel DE $\therefore m_{GF} = m_{DE} = 1$ $\therefore y = x + c$ (4; 2): $2 = 4 + c$ $c = -2$ $\therefore y = x - 2$ | ✓ $m_{GF} = 1$ ✓ subst/ vervang F(4; 2) ✓ Answer/ Antwoord | (3) | R |
| 3.1.5 | G(8; 6) | ✓ x; ✓ y | (2) | R |
| 3.1.6 | $ED = \sqrt{(-2 - 2)^2 + (-1 - 3)^2}$ $= \sqrt{32}$ $\frac{EF}{ED} = \frac{\sqrt{45}}{\sqrt{32}}$ $= \frac{3\sqrt{5}}{4\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} = \frac{3\sqrt{10}}{8}$ | ✓ subst/ vervang in ED ✓ Answer/ Antwoord ✓ $\frac{EF}{ED}$ ✓ $\times \frac{\sqrt{2}}{\sqrt{2}}$ | (4) | C |

| | | | | | | | | | | | | | | | | | | | | |
|-----------------------------------|---|---|------------------------|-----------------------------------|----------------|---------------------------|-----------------------------|------------------------|--|-------------------|--|---------------------|--|--------------------|--|----------------------|--|--|-----|---|
| 3.1.7 | $x^2 + y^2 = 45$ | <ul style="list-style-type: none"> ✓ x^2 ; ✓ y^2 or centre (0; 0) ✓ 45 | (3) | C | | | | | | | | | | | | | | | | |
| 3.2.1 | <p>AD \parallel x-axis/ as</p> <p>$\therefore \tan \theta = \frac{3}{2}$</p> <p>$\theta = 56,31^\circ$</p> | <ul style="list-style-type: none"> ✓ $\tan \theta = \frac{3}{2}$ ✓ Answer/ <i>Antwoord</i> | (2) | R | | | | | | | | | | | | | | | | |
| 3.2.2 | <p>Let A be the point/ <i>Laat A die punt</i> $(x; \frac{3}{2}x)$ <i>wees</i></p> <p>$\therefore D(5; \frac{3}{2}x)$</p> <p>AD² = DC² OR AD = DC</p> <table style="border-collapse: collapse; margin-left: 40px;"> <tr> <td style="border-right: 1px solid black; padding-right: 10px;">$(5 - x)^2 = (\frac{3}{2}x)^2$</td> <td style="padding-left: 10px;">$5 - x = \frac{3}{2}x$</td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 10px;">$25 - 10x + x^2 = \frac{9}{4}x^2$</td> <td style="padding-left: 10px;">$10 - 2x = 3x$</td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 10px;">$4x^2 - 40x + 100 = 9x^2$</td> <td style="padding-left: 10px;">$10 = 5x \Rightarrow x = 2$</td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 10px;">$0 = 5x^2 + 40x - 100$</td> <td></td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 10px;">$= x^2 + 8x - 20$</td> <td></td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 10px;">$= (x - 2)(x + 10)$</td> <td></td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 10px;">$\therefore x = 2$</td> <td></td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 10px;">$\therefore A(2; 3)$</td> <td></td> </tr> </table> | $(5 - x)^2 = (\frac{3}{2}x)^2$ | $5 - x = \frac{3}{2}x$ | $25 - 10x + x^2 = \frac{9}{4}x^2$ | $10 - 2x = 3x$ | $4x^2 - 40x + 100 = 9x^2$ | $10 = 5x \Rightarrow x = 2$ | $0 = 5x^2 + 40x - 100$ | | $= x^2 + 8x - 20$ | | $= (x - 2)(x + 10)$ | | $\therefore x = 2$ | | $\therefore A(2; 3)$ | | <ul style="list-style-type: none"> ✓ method/ <i>metode</i> ✓ equate lengths/ <i>stel lengtes =</i> ✓ standard form/ <i>standaardv</i> ✓ x ✓ y | (5) | P |
| $(5 - x)^2 = (\frac{3}{2}x)^2$ | $5 - x = \frac{3}{2}x$ | | | | | | | | | | | | | | | | | | | |
| $25 - 10x + x^2 = \frac{9}{4}x^2$ | $10 - 2x = 3x$ | | | | | | | | | | | | | | | | | | | |
| $4x^2 - 40x + 100 = 9x^2$ | $10 = 5x \Rightarrow x = 2$ | | | | | | | | | | | | | | | | | | | |
| $0 = 5x^2 + 40x - 100$ | | | | | | | | | | | | | | | | | | | | |
| $= x^2 + 8x - 20$ | | | | | | | | | | | | | | | | | | | | |
| $= (x - 2)(x + 10)$ | | | | | | | | | | | | | | | | | | | | |
| $\therefore x = 2$ | | | | | | | | | | | | | | | | | | | | |
| $\therefore A(2; 3)$ | | | | | | | | | | | | | | | | | | | | |
| | | | [24] | | | | | | | | | | | | | | | | | |

QUESTION/ VRAAG 4

| # | Suggested answer(s)/ <i>Voorgestelde antwoord(e)</i> | Descriptors/ <i>Beskrywers</i> | Mark/ <i>Punt</i> |
|-------|--|--|-------------------|
| 4.1 | $x^2 - 10x + y^2 + 6y - 2 = 0$ $(x^2 - 10x + 25) + (y^2 + 6y + 9) = 2 + 25 + 9$ $(x - 5)^2 + (y + 3)^2 = 36$ <p style="text-align: center;">Centre/ <i>Middelpt</i> (5; -3)</p> | <ul style="list-style-type: none"> ✓ LHS/ <i>LK</i>: +25 + 9 ✓ RHS/ <i>RK</i>: +25 + 9 ✓ equation/ <i>vergelyking</i> ✓ x; ✓ y | (5) R |
| 4.2.1 | $G(0; \frac{8}{5})$ | <ul style="list-style-type: none"> ✓ x ✓ y | (2) K |
| 4.2.2 | <p>Area/ <i>Oppervlakte</i> = $\frac{1}{2} \times EF \times OG$</p> $= \frac{1}{2} \times 2 \left(\frac{8}{5}\right) \times \frac{8}{5}$ $= \frac{64}{25} \text{ units}^2 / \text{eenhede}^2$ | <ul style="list-style-type: none"> ✓ substitute/ <i>vervanging</i> ✓ Answer/ <i>Antwoord</i> | (2) R |
| 4.2.3 | <p>$m_{MA} = \frac{2}{5}$ [radius \perp tangent/ <i>raaklyn</i>]</p> <p>$\therefore y = \frac{2}{5}x + c$</p> <p>$\therefore y = \frac{2}{5}x - 4$</p> | <ul style="list-style-type: none"> ✓ $m = \frac{2}{5}$ ✓ equation/ <i>vergelyking</i> | (2) R |

| | | | | |
|-------|---|--|------|---|
| 4.2.4 | $-3 = \frac{2}{5}a - 4 \quad \text{OR} \quad m_{rad} = \frac{-3-(-4)}{a-0} = \frac{2}{5} = \frac{1}{a}$ $\therefore a = 2\frac{1}{2}$ $r^2 = \left(2\frac{1}{2} - 0\right)^2 + (-3 + 4)^2 \quad \text{OR} \quad \left(2\frac{1}{2} - 5\right)^2 + (-3 + 2)^2$ $= 7,25$ $\therefore \left(x - 2\frac{1}{2}\right)^2 + (y + 3)^2 = 7,25$ <p>OR/ OF</p> $MA^2 = MB^2$ $a^2 + (-3 + 4)^2 = (a - 5)^2 + (-3 + 2)^2$ $a^2 + 1 = a^2 - 10a + 25 + 1$ $10a = 25$ $a = 2\frac{1}{2}$ $\therefore r^2 = \left(2\frac{1}{2}\right)^2 + 1$ $= 7,25$ $\therefore \left(x - 2\frac{1}{2}\right)^2 + (y + 3)^2 = 7,25$ | ✓ substitute/ <i>vervang</i> ✓ <i>a</i> ✓ r^2 ✓ equation/ <i>vergelyking</i> ✓ substitute/ <i>vervang</i> ✓ <i>a</i> ✓ r^2 ✓ equation/ <i>vergelyking</i> | (4) | |
| | | | (4) | C |
| | | | [15] | |

QUESTION/ VRAAG 5

| # | Suggested answer(s)/ <i>Voorgestelde antwoord(e)</i> | Descriptors/ <i>Beskrywers</i> | Mark/ <i>Punt</i> | |
|-------|--|--|----------------------|---|
| 5.1 | $\sin(90^\circ + x) \cdot \cos(-x) - \cos(180^\circ - x) \tan(x - 180^\circ) \cdot \sin(x)$ $= \cos x \cos x - (-\cos x) (\tan x) (\sin x)$ $= \cos^2 x - (-\cos x) \left(\frac{\sin x}{\cos x}\right) \sin x$ $= \cos^2 x + \sin^2 x$ $= 1$ | ✓ ✓ $\cos x$; $\cos x$ ✓ $-\cos x$ ✓ $\frac{\sin x}{\cos x}$ or $\tan x$ ✓ Answer/ <i>Antwoord</i> | (5) | R |
| 5.2.1 | $\sin 56^\circ = \sin(42 + 14) = \sin 42^\circ \cdot \cos 14^\circ + \cos 42^\circ \cdot \sin 14^\circ$ $= a + b$ | ✓ Expand/ <i>Uitbrei</i> ✓ Answer/ <i>Antwoord</i> | (2) | C |
| 5.2.2 | $\sin 28^\circ = \sin(42 - 14) = \sin 42^\circ \cdot \cos 14^\circ - \cos 42^\circ \cdot \sin 14^\circ$ $= a - b$ | ✓ Expand/ <i>Uitbrei</i> ✓ Answer/ <i>Antwoord</i> | (2) | C |
| 5.2.3 | $\cos 56^\circ$ $= \cos(2 \times 28^\circ)$ $= 1 - 2\sin^2 28^\circ$ $= 1 - 2(a - b)^2$ $= 1 - 2(a^2 - 2ab + b^2)$ $= 1 - 2a^2 + 4ab - 2b^2$ | ✓ $\cos(2 \times 28^\circ)$ ✓ Expansion/ <i>Uitbreiding</i> ✓ Substitute/ <i>Vervang</i> ($a - b$) | (3) | C |

Memo

| | | | | |
|-------|---|---|------|---|
| 5.3.1 | $\frac{\cos 2\theta + \sin^2 \theta}{1 + \sin \theta} = 1 - \sin \theta$ $LHS = \frac{\cos^2 \theta - \sin^2 \theta + \sin^2 \theta}{1 + \sin \theta}$ $= \frac{\cos^2 \theta}{1 + \sin \theta}$ $= \frac{1 + \sin \theta}{1 - \sin^2 \theta}$ $= \frac{1 + \sin \theta}{(1 - \sin \theta)(1 + \sin \theta)}$ $= \frac{1 + \sin \theta}{1 + \sin \theta}$ $= 1 - \sin \theta = RHS$ | <ul style="list-style-type: none"> ✓ $\cos^2 \theta - \sin^2 \theta$ ✓ Simplify/ Vereenvoudig ✓ $\cos^2 \theta = 1 - \sin^2 \theta$ ✓ Factorise/ Faktoreiseer | (4) | C |
| 5.3.2 | $\sin \theta = -1$ $\theta = 270^\circ + k \cdot 360^\circ \text{ for / vir } k \in \mathbb{Z}$ | <ul style="list-style-type: none"> ✓ equation/ vergelyking ✓ Answer/ Antwoord | (2) | R |
| 5.4 | $(\cos \theta + 2)^2 + (\sin \theta - 1)^2 = (\sqrt{6})^2$ $\cos^2 \theta + 4 \cos \theta + 4 + \sin^2 \theta - 2 \sin \theta + 1 = 6$ $1 + 4 \cos \theta - 2 \sin \theta + 5 = 6$ $-2 \sin \theta = -4 \cos \theta$ $\frac{\sin \theta}{\cos \theta} = 2$ $\tan \theta = 2$ | <ul style="list-style-type: none"> ✓ Substitution/ vervanging ✓ Simplify/ Vereenvoudig ✓ Answer/ Antwoord | (3) | P |
| | | | [21] | |

QUESTION/ VRAAG 6

| # | Suggested answer(s)/ Voorgestelde antwoord(e) | Descriptors/ Beskrywers | Mark /Punt | |
|-----|--|--|------------|---|
| 6.1 | $\sin x = \cos 2x - 1$ $\sin x = 1 - 2 \sin^2 x - 1$ $2 \sin^2 x + \sin x = 0$ $\sin x (2 \sin x + 1) = 0$ $\sin x = 0 \quad \text{or/ of } \sin x = -\frac{1}{2}$ $x = 0^\circ + k \cdot 360^\circ \quad \text{OR} \quad x = 210^\circ + k \cdot 360^\circ$ $x = 180^\circ + k \cdot 360^\circ \quad x = 330^\circ + k \cdot 360^\circ / -30^\circ + k \cdot 360^\circ$ $\therefore x = -180^\circ; -150^\circ; -30^\circ; 0^\circ$ | <ul style="list-style-type: none"> ✓ $1 - 2 \sin^2 x$ ✓ Standard form/ Standaardvorm ✓ $\sin x = 0$ or $\sin x = -\frac{1}{2}$ ✓✓ General solution/ Algemene <i>Oplissing [1 from each group/ block]</i> ✓ Answer/ Antwoord | (6) | C |

Memo

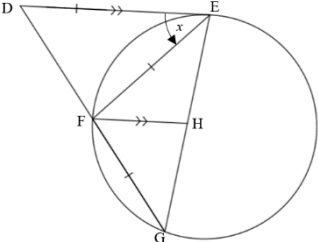
| | | | | |
|-------------|------------------------------------|--|-----|---|
| 6.2.1 | | ✓ x-intercept/ afsnit $(-90^\circ; 0)$ ✓ $(-180^\circ; 1)$ and/ en $(0; 1)$ | (2) | R |
| 6.2.2 | $h(x) = -\sin x - 1$ | ✓ Answer/ Antwoord | (1) | K |
| 6.2.3 | $-180^\circ \leq x \leq -90^\circ$ | ✓ endpoints/ eindpunte ✓ inequality notation/ ongelykheidsnotasie | (2) | P |
| [11] | | | | |

QUESTION/ VRAAG 7

| # | Suggested answer(s)/ Voorgestelde antwoord(e) | Descriptors/ Beskrywers | Mark/ Punt | |
|------------|--|---|------------|---|
| 7.1 | $\cos(90^\circ - x) = \frac{PA}{3}$ $\sin x = \frac{PA}{3}$ $PA = 3 \sin x$ | ✓ Reduction/ Reduksie – $\sin x$ ✓ Answer/ Antwoord | (2) | R |
| 7.2 | $In \Delta PAT: \frac{\sin(90^\circ + x)}{PT} = \frac{\sin 2x}{PA}$ $\frac{\cos x}{PT} = \frac{2 \sin x \cdot \cos x}{3 \sin x}$ $PT = \frac{3 \sin x \cos x}{2 \sin x \cos x}$ $= \frac{3}{2}$ Yes, they are 1,5m apart/ Ja, hulle is 1,5m van mekaar | ✓ Subst / vervang in sin rule/ reël ✓ expansion/ uitbreiding: $\sin 2x$ ✓ Answer/ Antwoord ✓ Conclusion/ Afleiding | (4) | C |
| 7.3 | $\therefore \widehat{APT} = 30^\circ$ $Area/Oppervlakte \Delta PAT = \frac{1}{2}(PA)(PT) \sin 30^\circ$ $= \frac{1}{2}(3 \sin 20^\circ) \left(\frac{3}{2}\right) \left(\frac{1}{2}\right)$ $= 0,38 m^2$ | ✓ \widehat{APT} ✓ Subst/ Vervang in Area rule/ reël ✓ Answer/ Antwoord | (3) | R |
| [9] | | | | |

QUESTION/ VRAAG 8

| # | Suggested answer(s)/ Voorgestelde antwoord(e) | Descriptors/ Beskrywers | Mark/Punt |
|-------|--|---|-----------|
| 8.1 | | | |
| | <p>Construction/ <i>Konstruksie</i>: Draw CO produced/ <i>Trek CO verleng</i> Proof/ <i>bewys</i>: $\hat{C}_1 = \hat{A}$ [\angles opposite = sides/ \anglee teenoor = sye] $\therefore \hat{O}_1 = 2\hat{C}_1$ [ext. \angle of Δ/ <i>buite \angle van Δ</i>] Similarly/ <i>Netso</i>: $\hat{O}_2 = 2\hat{C}_2$ Now/ <i>Nou</i>: $\hat{O}_1 + \hat{O}_2 = 2\hat{C}_1 + 2\hat{C}_2$ $\therefore \hat{AOB} = 2(\hat{C}_1 + \hat{C}_2)$ $= 2\hat{ACB}$</p> | <p>✓ Construction/ <i>Konstruksie</i> ✓ S/ R ✓ S/ R ✓ S (Similarly/ <i>Netso</i>) ✓ S (any/ <i>enige 1</i>)</p> | (5) K |
| 8.2 | | | |
| 8.2.1 | (a) $\hat{A}_1 = 35^\circ$ [tan- chord thm/ <i>raakl-koordstelling</i>] | ✓ S ✓ R | (2) K |
| | (b) $\hat{O}_3 = 70^\circ$ [\angle at centre = 2 \angle at circumf/ <i>middelpts \angle = 2 omtr. \angle</i>] | ✓ S ✓ R | (2) K |
| | (c) $\hat{P}_3 = 55^\circ$ [Σ interior/ <i>binne \angle of/ van (isosceles/gelykbenige) Δ</i>] | ✓ S ✓ R | (2) K |
| | (d) $\hat{BOM} = 90^\circ$ [adjacent/ <i>aanligg – suppl.</i>] And/ <i>en</i> $\hat{OBM} = 55^\circ$ [Σ \angle s of/ <i>van (isosceles/gelykbenige) Δ</i>] OR/ OF [\angle s opposite = radii/ sides/ \angle e teenoor = <i>radiusse/ sye</i>] OR/OF $\hat{OBS} = 90^\circ$ [tan/ <i>raakl. \perp radius</i>] $\therefore \hat{M}_1 = 35^\circ$ [Σ \angle s of/ <i>van Δ</i>] OR/OF $\hat{APB} = 90^\circ$ [\angle in semi circle/ \angle in <i>halwe sirkel</i>] $\therefore \hat{P}_1 = 90^\circ$ [adj./ <i>aanligg./ suppl</i>] $= \hat{O}_1$ AMPO is cycl quad/ <i>is 'n kvh</i> [conv. \angle s Subt by same chord/ <i>omg. \anglee ondersp. deur selfde koord</i>] $\therefore \hat{M}_1 = \hat{A}_1 = 35^\circ$ [\angle s Subt by same chord/ \angle e <i>ondersp. deur selfde koord</i>] | <p>✓ S/ R ✓ S/ R ✓ S</p> | (3) K |
| 8.2.2 | (a) $\hat{APB} = 90^\circ$ [\angle in semi-circle/ \angle in <i>halwe sirkel</i>] $= \hat{O}_1$ [Given/ <i>Gegee</i>] \therefore OLPB is a cycl. quad/ <i>is 'n kvh</i> [ext \angle =opp. int \angle / <i>buite \angle=teenoorst. binne \angle</i>] | <p>✓ S ✓ R ✓ R</p> | (3) R |

| | | | | |
|-----------------------------|---|--|------------|-------------------|
| <p>9.2.3</p> | <p><u>In $\triangle DGE$ and/ en $\triangle DEF$:</u></p> <ol style="list-style-type: none"> \hat{D} is common/ <i>gemeen</i> $\hat{G} = \hat{D}EF = x$ [proved/ <i>bewys</i>] $\therefore \hat{D}EG = \hat{D}FE$ [3^{rd}/ 3^{de} \angle] <p>$\therefore \triangle DGE \parallel \triangle DEF$ [\angle, \angle, \angle]</p> | <p>✓ S ✓ S ✓ S OR/ <i>OF</i> ✓ R (\angle, \angle, \angle) (Can also work with 72° etc)</p> | <p>(3)</p> | <p>R</p> |
| <p>9.2.4</p> | <p>$\therefore \frac{DG}{DE} = \frac{GE}{EF} = \frac{DE}{DF}$ from/ <i>vanaf</i> 9.2.3 OR/ <i>OF</i> $\triangle DGE \parallel \triangle DEF$</p> <p>$\Rightarrow DE^2 = DF \cdot DG$</p> | <p>✓ S ✓ R Can only give needed 2 ratios</p> | <p>(2)</p> | <p>K</p> |
| <p>9.2.5</p> | <p>$\frac{DE}{DF} = \frac{DG}{DE}$</p> <p>$\frac{1}{y} = \frac{DF+FG}{DE}$</p> <p>$= \frac{DF}{DE} + \frac{FG}{DE}$</p> <p>$= y + 1$</p> <p>$\therefore y^2 + y = 1$</p> | <p>✓ S Correct Proportion/ Korrekte Eweredigheid</p> <p>✓ $\frac{DE}{DF} = \frac{1}{y}$ ✓ $\frac{DG}{DE} = \frac{DF+FG}{DE}$ ✓ $\frac{1}{y} = \frac{DF}{DE} + \frac{FG}{DE}$ ✓ $\frac{FG}{DE} = 1$</p> | <p>(5)</p> | <p>P</p> |
| <p>9.2.6</p> | <p>In $\triangle DEF$: $EF^2 = DF^2 + DE^2 - 2 DF \cdot DE \cdot \cos D$</p> <p>$\therefore \cos D = \frac{DF^2 + DE^2 - EF^2}{2 DF \cdot DE}$</p> <p>$= \frac{DF^2}{2 DF \cdot DE} = \frac{DF}{2 DE}$</p> <p>$\therefore \cos 72^\circ = \frac{1}{2} y$</p>  | <p>✓ cos rule/ <i>reël</i> for/ <i>vir</i> $\triangle DEF$</p> <p>✓ $DE^2 - EF^2 = 0$</p> <p>✓ Simplify/ <i>Vereenvoudig</i></p> | <p>(3)</p> | <p>P</p> |
| <p>[27]</p> | | | | |
| <p>TOTAL/ TOTAAL</p> | | | | <p>150</p> |