



Education

KwaZulu-Natal Department of Education
REPUBLIC OF SOUTH AFRICA

MATHEMATICS P2

PREPARATORY EXAMINATION

SEPTEMBER 2016

MEMORANDUM

**NATIONAL
SENIOR CERTIFICATE**

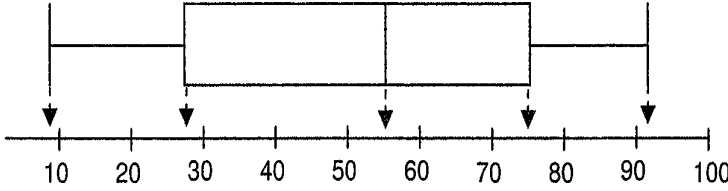
GRADE 12

MARKS : 150

This memorandum consists of 15 pages.

SECTION A

QUESTION 1

<p>1.1 min = 9 ; maximum = 92 ; upper quartile = 75 Lower quartile = 28 and medium = 55 Therefore five number summary is (9; 28; 55; 75; 92)</p>	<p>A✓9 and 92 A✓28 A✓55 A✓75 (4)</p>
<p>1.2</p> 	<p>CA✓ correct Q1 & Q3 CA✓ median correctly shown CA✓ both correct whiskers (3)</p>
<p>1.3 Data is skewed to the left /Data is negatively skewed</p>	<p>CA CA✓✓ Answer (2)</p>
<p>1.4 mean mark for M-cee-nai High</p> $= \frac{9+14+14+19+21+23+33+35+37+37+42+45+55+56+57+59+68+75+75+75+77+78+80+81+92}{25}$ $\frac{1257}{25} = 50,28$ <p>OR</p> $\bar{x} = \frac{1257}{25} = 50,28$	<p>A✓ sum CA✓ answer (2) [Answer only full marks]</p>
<p>1.5 Bee Vee High School. Bee Vee High School performed better because half of the learners got above 60% whilst half of M-cee-nai learners got more than 55%. The median of Bee Vee High was higher than that of M-cee-nai High.</p>	<p>CA✓ Bee Vee High CA✓✓ Reasoning (3)</p>
	<p>[13]</p>

QUESTION 2

2.1	(6; 160)	A✓ 6 A✓ 160	(2)
2.2	$y = -1,64x + 73,52$	AA✓✓ gradient AA✓✓ y - intercept	(4)
2.3	$r = -0,2$	AA✓✓ answer	(2)
			[8]

QUESTION 3

3.1	$AC = \sqrt{(-5-7)^2 + (1-(2))^2}$ $= \sqrt{(12)^2 + (3)^2}$ $= \sqrt{144 + 9}$ $= \sqrt{153}$ $= 12,37$	A✓ correct Subst CA ✓ answer	(2)
3.2	$M_{BC} = \frac{6-(2)}{1-7}$ $= \frac{8}{-6}$ $= \frac{-4}{3}$ $y - y_1 = m(x - x_1)$ $y - 6 = -\frac{4}{3}(x - 1)$ $3y - 18 = -4x + 4$ $3y = -4x + 22$	A✓ $\frac{-4}{3}$ CA✓ correct subst. of (1;6) And (7;-2) CA✓ equation in any form	(3)

<p>3.3 $\hat{B} = \theta = \alpha - \beta$...Ext \angle</p> $\tan \alpha = m_{BC} = -\frac{4}{3}$ $\therefore \alpha = 126,9^\circ$ $\tan \beta = m_{AB} = \frac{5}{6}$ $\therefore \beta = 39,8^\circ$ $\theta = \alpha - \beta$ $\theta = \alpha - \beta$ $= 126,9^\circ - 39,8^\circ$ $= 87,1^\circ$ $\therefore \hat{ABC} = 87,1^\circ$ <p>OR</p> $\text{Distance AB} = \sqrt{(1+5)^2 + (6-1)^2}$ $= \sqrt{61}$ $\text{Distance BC} = \sqrt{(1-7)^2 + (6+2)^2}$ $= \sqrt{100}$ $= 10$ $\text{Distance AC} = \sqrt{(-5-7)^2 + (1+2)^2}$ $= \sqrt{153}$ $\cos \hat{B} = \frac{a^2 + c^2 - b^2}{2ac}$ $= \frac{10^2 + (\sqrt{61})^2 - (\sqrt{153})^2}{2(10)(\sqrt{61})}$ $= 0,051$ $\hat{B} = 87,1^\circ$	<p>CA ✓ $\tan \alpha = -\frac{4}{3}$</p> <p>CA ✓ $\alpha = 126,9^\circ$</p> <p>A ✓ $\tan \beta = \frac{5}{6}$</p> <p>CA ✓ $\beta = 39,8^\circ$</p> <p>CA ✓ $\hat{ABC} = 87,1^\circ$</p> <p>(5)</p> <p>A ✓ Distance AB</p> <p>A ✓ Distance BC</p> <p>A ✓ Distance AC</p> <p>CA ✓ substitution in cosine rule</p> <p>CA ✓ answer</p> <p>(5)</p>
<p>3.4 $P\left(\frac{-5+1}{2}; \frac{1+6}{2}\right)$</p> $P\left(-2; \frac{7}{2}\right)$	<p>AA ✓ ✓ both co-ordinates</p> <p>(2)</p>

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<p>3.5 $m_{AC} = \frac{-2-1}{7+5}$</p> $= \frac{-3}{12}$ $= \frac{-1}{4}$ <p>through $(-1 ; 3)$</p> <p>equation: $y - 3 = -\frac{1}{4}(x + 1)$</p> $y - 3 = -\frac{1}{4}x - \frac{1}{4}$ <p>$\therefore y = \frac{-1}{4}x + 2\frac{3}{4}$ or $y = -\frac{1}{4}x + \frac{11}{4}$ or</p> $4y + x - 11 = 0$	<p>A ✓ $\frac{-1}{4}$</p> <p>CA ✓ subst. $(-1;3)$</p> <p>CA ✓ equation.in any form</p> <p>(3)</p>
<p>3.6 $m_{AB} = \frac{5}{6}; 6x + 5y = 18$</p> $5y = -6x + 18$ $y = \frac{-6}{5}x + \frac{18}{5}$ <p>$\therefore m_1 = \frac{-6}{5}$</p> $m_{AB} m_1 = -1$ <p>$\therefore m_{AB} \perp 6x + 5y = 18$</p>	<p>A ✓ $m_1 = -\frac{6}{5}$</p> <p>A ✓ $m_{AB} \cdot m_1$</p> <p>A ✓ $= -1$</p> <p>(3)</p>
	[18]

<p>QUESTION 4</p> <p>4.1.1 At W, $y = 2$ $3x + 4(2) + 7 = 0$ $3x = -15$ $x = -5$ W(-5;2) $r = 5$ $(x + 5)^2 + (y - 2)^2 = 25$</p>	<p>A✓ subst $y = 2$</p> <p>CA ✓ $x = -5$</p> <p>CA✓ co -ordinates of W</p> <p>CA✓ $r = 5$</p> <p>CA✓ equation of the circle.</p> <p>(5)</p>
<p>4.1.2 $VZ = 2r = 2 \times 5 = 10$ units</p>	<p>CA✓ answer (1)</p>
<p>4.1.3 $m_{GZ} = \frac{2+1}{0+1}$ $= 3$</p>	<p>A✓ substitution into formula</p> <p>CA✓ answer (2)</p>
<p>4.1.4 Midpoint of GZ is $\left(-\frac{1}{2}; \frac{1}{2}\right)$</p>	<p>A✓ coordinates (1)</p>
<p>4.1.5 $m_{GZ} = 3$ $m_{\perp} = -\frac{1}{3}$ $y - \frac{1}{2} = -\frac{1}{3}\left(x + \frac{1}{2}\right)$ $y = -\frac{1}{3}x + \frac{1}{3}$</p>	<p>CA✓ gradient of perpendicular bisector</p> <p>CA✓ substitution into formula</p> <p>CA ✓ answer (3)</p>

<p>4.1.6 W (-5; 2) into $x + 3y - 1 = 0$</p> $\begin{aligned} \text{LHS} &= (2(-5) + 6(2) - 2) \\ &= -10 + 12 - 2 \\ &= 0 \\ &= \text{RHS} \end{aligned}$ <p>W is on the line that bisects GZ perpendicularly and W on GZ. \therefore lines intersect at W.</p> <p>OR</p> $\begin{aligned} -\frac{1}{3}x + \frac{1}{3} &= 2 \\ -x + 1 &= 6 \\ x &= -5 \end{aligned}$ <p>This is the x - value of the coordinate of W.</p> <p>OR</p> <p>Equation of WZ:</p> $\begin{aligned} y - y_1 &= m(x - x_1) \\ y + 1 &= \frac{2+1}{-5+1}(x+1) \\ y + 1 &= -\frac{3}{4}(x+1) \\ y &= -\frac{3}{4}x - \frac{7}{4} \\ \therefore -\frac{3}{4}x - \frac{7}{4} &= -\frac{1}{3}x + \frac{1}{3} \\ -9x - 21 &= -4x + 4 \\ -5x &= 25 \\ x &= -5 \\ \therefore y &= -\frac{1}{3}(-5) + \frac{1}{3} = 2 \end{aligned}$ <p>This is the coordinate of W.</p>	<p>A✓ substitution</p> <p>A✓ = 0</p> <p>(2)</p> <p>A✓ equating eq. of perpendicular bisector to the horizontal line $y = 2$</p> <p>A✓ $x = -5$</p> <p>(2)</p> <p>A✓ equation of WZ</p> <p>A✓ $x = -5$</p> <p>(2)</p>
<p>4.2.1 circle M: M(-2; 1) ; $r_1 = 5$ circle N: N(1;3) ; $r_2 = 3$ $\therefore r_1 + r_2 = 8$ and $r_1 - r_2 = 2$</p> $\begin{aligned} \text{MN} &= \sqrt{(1-(-2))^2 + (3-1)^2} \\ &= \sqrt{3^2 + 2^2} \\ &= \sqrt{9 + 4} \\ &= \sqrt{13} \text{ or } 3,6 \end{aligned}$ <p>$\therefore r_1 + r_2 > \text{MN} > r_1 - r_2$ \therefore The two circles intersect at two distinct points.</p>	<p>A ✓ $r_1 = 5$ A ✓ $r_2 = 3$ A ✓ $r_1 + r_2 = 8$</p> <p>A ✓ $\text{MN} = \sqrt{13}$ = 3,6</p> <p>A✓ comparing A✓ conclusion (6)</p>

<p>4.2.2</p> <p>circle M = circle N</p> $(x + 2)^2 + (y - 1)^2 - 25 = (x - 1)^2 + (y - 3)^2 - 9$ $x^2 + 4x + 4 + y^2 - 2y + 1 - 25 = x^2 - 2x + 1 + y^2 - 6y + 9 - 9$ $6x + 4y = 21$ <p>∴ The equation of the common chord is :</p> $6x + 4y = 21$	<p>M✓ equating</p> <p>A✓ simplifying</p> <p>CA✓ equation of the chord</p> <p>(3)</p> <p>[23]</p>
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<p>QUESTION 5</p> <p>5.1.1 $\tan \alpha = \frac{-2}{2\sqrt{3}} = \frac{-1}{\sqrt{3}}$</p> <p>∴ $\alpha = 360^\circ - 30^\circ$</p> <p style="padding-left: 40px;">$= 330^\circ$</p> <p>∴ $\beta = 30^\circ$</p> <p style="padding-left: 100px;">or</p> <p>$\tan(-\beta) = -\tan \beta$</p> $= -\left(\frac{-2}{2\sqrt{3}}\right)$ <p>$\tan \beta = \frac{2}{2\sqrt{3}}$</p> <p>$\beta = 30^\circ$</p>	<p>A✓ correct ratio</p> <p>CA✓ $\alpha = 330^\circ$</p> <p>CA✓ $\beta = 30^\circ$</p> <p>A✓ correct ratio</p> <p>CACA✓✓ $\beta = 30^\circ$</p> <p>(3)</p>
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<p>5.1.2 $OP^2 = (2\sqrt{3})^2 + (-2)^2 = 12 + 4$</p> <p style="padding-left: 40px;">$= 16$</p> <p>∴ $OP = 4$</p>	<p>A✓ using distance for formula</p> <p>CA✓ answer</p> <p>(2)</p>
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<p>5.1.3 $\frac{OP}{OQ} = \cos \beta$</p> <p>∴ $OQ = \frac{OP}{\cos \beta} = \frac{4}{\cos 30^\circ}$</p> $= \frac{4}{\frac{\sqrt{3}}{2}}$ $= \frac{8}{\sqrt{3}}$	<p>CA✓ $\cos 30^\circ = \frac{\sqrt{3}}{2}$</p> <p>CA✓ $\frac{8}{\sqrt{3}}$</p>
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$Q = \left(\frac{8\sqrt{3}}{3}; 0 \right)$ <p style="text-align: center;">or</p> $\frac{OP}{OQ} = \cos 30^\circ$ $OQ = \frac{4}{\cos 30^\circ} = \frac{4}{\frac{\sqrt{3}}{2}}$ $OQ = \frac{8\sqrt{3}}{3}$ $Q = \left(\frac{8\sqrt{3}}{3}; 0 \right)$	<p>CA✓ co-ordinates</p> <p>CA✓ $\cos 30^\circ = \frac{\sqrt{3}}{2}$</p> <p>CA✓ $\frac{8\sqrt{3}}{3}$</p> <p>CA✓ co-ordinates</p> <p style="text-align: right;">(3)</p>
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<p>5.2 $2 \left[\frac{1}{2} \cos \alpha + \frac{\sqrt{3}}{2} \sin \alpha \right]$</p> <p>= $2 [\sin 30^\circ \cos \alpha + \cos 30^\circ \sin \alpha]$</p> <p>= $2 \sin (30^\circ + \alpha)$</p> <p>$k = 2; \beta = 30^\circ$</p> <p style="text-align: center;">OR</p> <p>$\frac{1}{2} \cos \alpha + \frac{\sqrt{3}}{2} \sin \alpha = \frac{k}{2} (\sin \alpha + \beta)$</p> <p>= $\sin 30^\circ \cos \alpha + \cos 30^\circ \sin \alpha = \frac{k}{2} \sin (\alpha + \beta)$</p> <p>= $\sin (30^\circ + \alpha) = \frac{k}{2} \sin (\alpha + \beta)$</p> <p>$\frac{k}{2} = 1, \beta = 30^\circ$</p> <p>$\therefore k = 2, \beta = 30^\circ$</p> <p>OR</p>	<p>M✓ for introducing 2</p> <p>A✓ introducing 30° special angle</p> <p>A✓ sum compound formula</p> <p>A✓ calculating k</p> <p>A✓ calculating β</p> <p>A✓ for introducing 2</p> <p>A✓ introducing 30° special angle</p> <p>A✓ sum compound formula</p> <p>A✓ calculating k</p> <p>A✓ calculating β</p> <p style="text-align: right;">(5)</p>
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$$\cos \alpha + \sqrt{3} \sin \alpha = k \sin(\alpha + \beta)$$

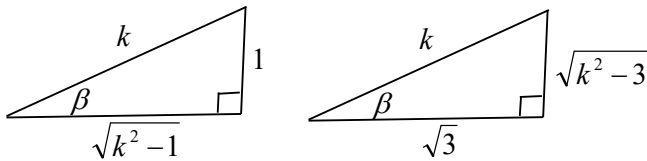
$$\cos \alpha + \sqrt{3} \sin \alpha = k(\sin \alpha \cos \beta + \cos \alpha \sin \beta)$$

$$\cos \alpha + \sqrt{3} \sin \alpha = k \sin \alpha \cos \beta + k \cos \alpha \sin \beta$$

$$\cos \alpha + \sqrt{3} \sin \alpha = (k \sin \beta) \cos \alpha + (k \cos \beta) \sin \alpha$$

$$\therefore 1 = k \sin \beta \quad \text{and} \quad \sqrt{3} = k \cos \beta$$

$$\therefore \sin \beta = \frac{1}{k} \quad \cos \beta = \frac{\sqrt{3}}{k}$$



$$\sqrt{k^2 - 1} = \sqrt{3}$$

$$k^2 = 4$$

$$k = 2$$

$$\sin \beta = \frac{1}{2}$$

$$\beta = 30^\circ$$

A✓ expansion

A✓ comparing coefficients

A✓ values of trig ratios

A✓ calculating k

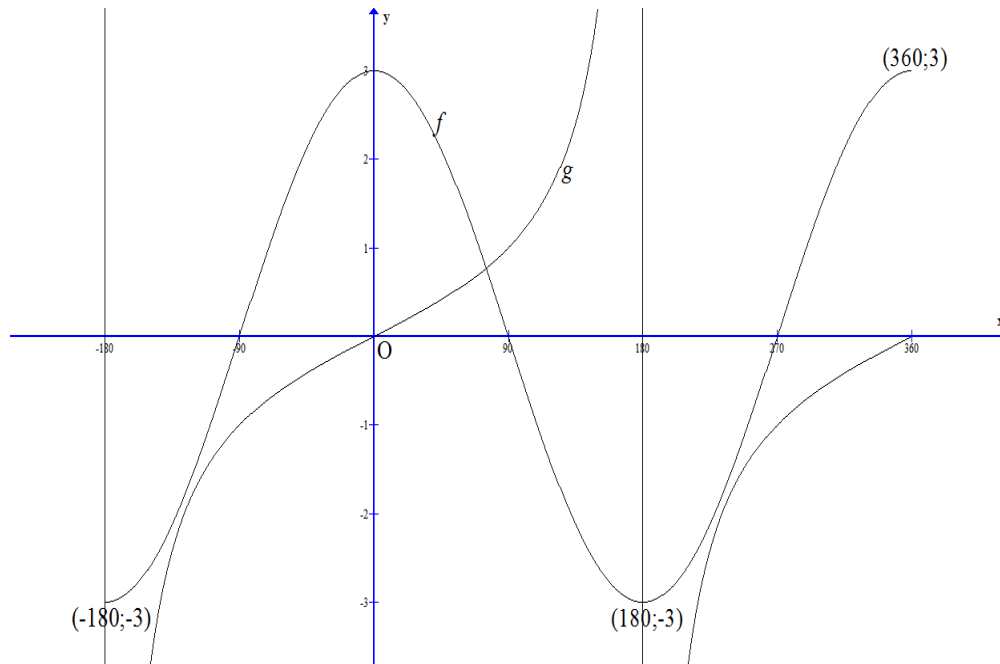
A✓ calculating β

(5)

[13]

QUESTION 6

6.1



A✓ asymptotes
A✓ shape of f
A✓ shape of g
A✓ correct x - intercept
of f (-90° ; 90° ; 270°)
A✓ correct x – intercept
of g (0° ; 360°)

(5)

6.2 360°

A✓ 360°

(1)

6.3 $(0; 3)$ and $(180^\circ ; -3)$
 $(-180^\circ ; -3)$ and $(360^\circ ; 3)$

CA✓ for any two

(2)

6.4 $-180^\circ < x < 0^\circ$ or $180^\circ < x < 360^\circ$
OR
 $-180^\circ < x < 0^\circ \cup 180^\circ < x < 360^\circ$

CA✓ $-180^\circ < x < 0^\circ$
CA✓ $180^\circ < x < 360^\circ$
[penalize one mark for
incorrect notation]

(2)

6.5 $y = 3\cos(x - 45^\circ)$

A✓ $3\cos(x - 45^\circ)$

(1)

[11]

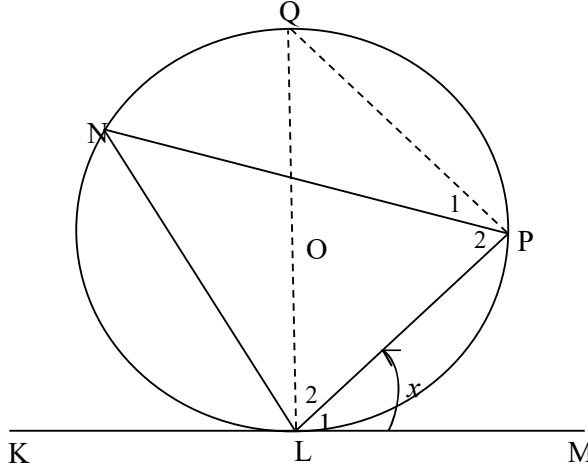
<p>QUESTION 7</p> <p>7.1 $\cos 54^\circ \cdot \cos x + \sin 54^\circ \cdot \sin x = \sin 2x$ $\cos(54^\circ - x) = \sin 2x$ $= \cos(90^\circ - 2x)$</p> <p>$\therefore 54^\circ - x = 90^\circ - 2x + n \cdot 360^\circ$ or $54^\circ - x = 360 - (90^\circ - 2x) + n \cdot 360^\circ$</p> <p>$x = 36^\circ + n \cdot 360^\circ$ or $-3x = 216^\circ + n \cdot 360^\circ$</p> <p>$x = 36^\circ + n \cdot 360^\circ$ or $-x = -72^\circ + n \cdot 120^\circ$</p> <p>$\therefore x = 36^\circ + n \cdot 360^\circ$ or $x = -72^\circ + n \cdot 120^\circ, n \in \mathbb{Z}$</p>	<p>A✓ $\cos(54^\circ - x)$ A✓ $\cos(90^\circ - 2x)$</p> <p>CA✓ $x = 36^\circ + n \cdot 360^\circ$ CA✓ $x = -72^\circ + n \cdot 120^\circ$</p> <p>A✓ $n \in \mathbb{Z}$ (5)</p>
<p>7.2.1 $\hat{E}FD = \hat{F}BC = \alpha$... corresponding \angle's ... $AD \parallel BC$</p> <p>$\hat{E}FD = \theta + \hat{A}EF$... ext \angle of $\triangle AEF$</p> <p>$\therefore \hat{A}EF = \alpha - \theta$</p> <p>In $\triangle ABE$: $\frac{\sin \hat{A}EB}{AB} = \frac{\sin \hat{E}AB}{BE}$</p> <p>$\therefore BE = \frac{AB \sin(90^\circ + \theta)}{\sin(\alpha - \theta)}$</p> <p>$= \frac{AB \cos \theta}{\sin(\alpha - \theta)}$</p>	<p>A✓ S/R A✓ S/R A✓ $\hat{A}EF = \alpha - \theta$</p> <p>A✓ sine rule application</p> <p>A✓ substitution (5)</p>
<p>7.2.2 Area of $\triangle BCE = \frac{1}{2} \cdot x(18 - 3x) \sin 150^\circ$</p> <p>$A(x) = \frac{1}{2} x \cdot (18 - 3x) \cdot \frac{1}{2}$</p> <p>$= \frac{1}{4} \cdot x \cdot 18 - \frac{1}{4} x \cdot 3x$</p> <p>$= \frac{18}{4} x - \frac{3}{4} x^2$</p> <p>$= \frac{9}{2} x - \frac{3}{4} x^2$</p>	<p>A✓ area rule</p> <p>A✓ $\sin 150^\circ = \frac{1}{2}$</p> <p>A✓ simplifying (3)</p>

<p>7.2.3 At maximum area: $A'(x) = 0$</p> $A'(x) = \frac{9}{2} - 2 \cdot \frac{3}{4}x$ $0 = \frac{9}{2} - \frac{3}{2}x$ $3x = 9$ $x = 3$	<p>M✓ $A'(x) = 0$</p> <p>A✓ derivative</p> <p>CA✓ $x = 3$ (3)</p>
<p>7.2.4</p> $BC = 3$ $CE = 18 - 3(3)$ $= 18 - 9$ $= 9$ $BE^2 = BC^2 + CE^2 - 2 BC \cdot CE \cos 150^\circ$ $= (3)^2 + (9)^2 - 2 \times 3 \times 9 (-\cos 30^\circ)$ $= 9 + 81 + 54 \cos 30^\circ$ $= 90 + 54 \cdot \left(\frac{\sqrt{3}}{2}\right)$ $= 136,765$ $\therefore BE = 11,695$ $= 11,69$	<p>A✓ for both $BC = 3$ and $CE = 9$</p> <p>CA✓ applying cosine rule and substitution</p> <p>CA✓ answer</p> <p>(3)</p> <p>[19]</p>

QUESTION 8

8.1 $PT = TQ = 12\text{cm}$...(line from center perpendicular to chord PQ) $\therefore PQ = 12\text{ cm} + 12\text{ cm} = 24\text{cm}$	$A\checkmark R$ $A\checkmark$ answer (2)
8.2 $OT^2 = OQ^2 - QT^2$ pythagoras $= 13^2 - 12^2$ $= 169 - 144$ $= 25$ $\therefore OT = 5$ $\therefore TR = OR - OT$ $= 13\text{cm} - 5\text{cm}$ $= 8\text{cm}$ In ΔPTR , $PR^2 = TR^2 + PT^2$ $= 8^2 + 12^2$ $= 64 + 144$ $= 208\text{ cm}^2$ $\therefore PR = \sqrt{208}\text{ cm}$ or $4\sqrt{13}\text{ cm}$ or 14,42 cm	$A\checkmark OT = 5$ $CA\checkmark TR = 8\text{cm}$ $CA\checkmark PR^2 = 208$ $CA\checkmark PR = 4\sqrt{13}$ or 14,42 (4) [6]

QUESTION 9

<p>9.1 Interior opposite angle</p>	<p>A✓ S (1)</p>														
<p>9.2</p>  <p>Construction : Draw diameter LOQ and join QP or Join OL and OP</p> <table border="1" data-bbox="276 892 1088 1228"> <thead> <tr> <th>STATEMENT</th> <th>REASON</th> </tr> </thead> <tbody> <tr> <td>Let $\hat{P}LM = \hat{L}_1 = x$</td> <td></td> </tr> <tr> <td>$\hat{P}_1 + \hat{P}_2 = 90^\circ$</td> <td>angle subtended by the diameter</td> </tr> <tr> <td>$\hat{L}_2 = 90^\circ - x$</td> <td>LM \perp OL, tan – radius</td> </tr> <tr> <td>$\therefore \hat{Q} = x$</td> <td>Sum of the angles of a triangle</td> </tr> <tr> <td>$\hat{N} = x$</td> <td>Subtended by the same chord LP</td> </tr> <tr> <td>$\hat{P}LM = \hat{N}$</td> <td></td> </tr> </tbody> </table>	STATEMENT	REASON	Let $\hat{P}LM = \hat{L}_1 = x$		$\hat{P}_1 + \hat{P}_2 = 90^\circ$	angle subtended by the diameter	$\hat{L}_2 = 90^\circ - x$	LM \perp OL, tan – radius	$\therefore \hat{Q} = x$	Sum of the angles of a triangle	$\hat{N} = x$	Subtended by the same chord LP	$\hat{P}LM = \hat{N}$		<p>A✓ construction</p> <p>A✓S/R A✓S/R A✓S A✓S/R</p> <p>(5)</p>
STATEMENT	REASON														
Let $\hat{P}LM = \hat{L}_1 = x$															
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$\hat{P}LM = \hat{N}$															
<p>9.3.1 $\hat{A} = 180^\circ - \hat{A}ED$... co interior \angle's, AB//ED $= 180^\circ - 70^\circ$ $= 110^\circ$</p>	<p>A✓ S/R</p> <p>A✓ 110° (2)</p>														
<p>9.3.2 $\hat{B}_1 = 70^\circ$... ext \angle cyclic quad ABDE</p>	<p>A✓ R</p> <p>A✓ 70° (2)</p>														
<p>9.3.3 $\hat{D}_2 = \hat{B}_1 = 70^\circ$(alt \angles ; DE//CA)</p>	<p>CA✓ 70°</p> <p>A✓ S/R (2)</p>														
<p>9.3.4 $\hat{B}_2 = \hat{D}_2 = 70^\circ$... (\angles opp = sides)</p>	<p>CA✓ 70°</p> <p>A✓ S/R (2)</p>														

<p>9.3.5 $\hat{E}_1 = 180^\circ - (\hat{B}_2 + \hat{D}_2) \dots (\angle \text{sum of } \Delta)$ $= 180^\circ - 140^\circ$ $= 40^\circ$ $\therefore \hat{D}_1 = \hat{E}_1 = 40^\circ \dots \text{tan chord theorem}$</p>	<p>CA✓ $\hat{E}_1 = 40^\circ$ CA✓ $\hat{D}_1 = 40^\circ$ A✓ R</p> <p style="text-align: right;">(3) [17]</p>
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QUESTION 10

<p>10.1 $\hat{P}_1 = \hat{B}_2 = x \dots \text{alt } \angle\text{s}; \text{SP//BC}$ $\hat{P}_2 = \hat{P}_1 = x \dots \text{given}$ $Q_1 = P_1 = x \dots \text{tan chord theorem}$</p>	<p>A✓ S A✓ R A✓ S/R A✓ S/R</p> <p style="text-align: right;">(4)</p>
<p>10.2 $PC = BC \dots \hat{P}_2 = \hat{B}_2 = x \dots \text{proved above}$ (ΔPCB)</p>	<p>A✓ $\hat{P}_2 = \hat{B}_2 = C = x$ A✓ reason</p> <p style="text-align: right;">(2)</p>
<p>10.3 $\hat{Q}_1 = \hat{B}_2 = x \dots \text{proved}$ $\therefore \text{RCQB is a cyclic quad}$ $\dots \text{converse } \angle\text{'s in the same segment}$</p>	<p>A✓ S A✓ R</p> <p style="text-align: right;">(2)</p>
<p>10.4 $\hat{S} = \hat{B}_3 \dots \text{corresp } \angle\text{'s SP} \parallel \text{BC}$ $= \hat{R}_3 \dots \angle\text{'s in the same segment, cyclic quad RCQB}$ In ΔPBS and ΔQCR $\hat{P}_1 = \hat{Q}_1 = x \dots \text{proved}$ $\hat{S} = \hat{R}_3 \dots \text{proved}$ Remaining $\angle\text{s equal}$ $\therefore \Delta PBS \parallel \Delta QCR$</p>	<p>A✓ S/R A✓ S/R A✓ S/R A✓ S/R A✓ R</p> <p style="text-align: right;">(5)</p>
<p>10.5 In ΔPBQ and ΔPCR \hat{P}_2 is common $\hat{PQB} = \hat{R}_2 \dots \text{ext } \angle \text{ of cyclic quad RCQB}$ $\Delta PBQ \parallel \Delta PCR \dots (3^{\text{rd}} \angle \Delta)$ $\therefore \frac{PB}{CP} = \frac{QB}{CR} (\parallel \Delta \text{s})$ $\therefore PB \cdot CR = QB \cdot CP$</p>	<p>A✓ S A✓ S/R A✓ S/R A✓ S</p> <p style="text-align: right;">(4) [17]</p>

QUESTION 11

<p>In ΔKLM $\frac{LD}{9} = \frac{8}{6} \dots$ (LM//DE; proportionality theorem) $\therefore LD = 12$ $\widehat{DML} = \widehat{MDE} = x \dots$ alt $\angle s$, LM \parallel DE $\therefore LM = LD = 12 \dots$ (sides opp = $\angle s$)</p>	<p>A✓S/R A✓LD = 12 A✓S A✓answer A✓R (5)</p>
	[5]

TOTAL: [150]