



basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

NATIONAL SENIOR CERTIFICATE

GRADE/GRAAD 12

MATHEMATICS P2/WISKUNDE V2

FEBRUARY/MARCH/FEBRUARIE/MAART 2015

MEMORANDUM

MARKS/PUNTE: 150

**This memorandum consists of 24 pages.
Hierdie memorandum bestaan uit 24 bladsye.**

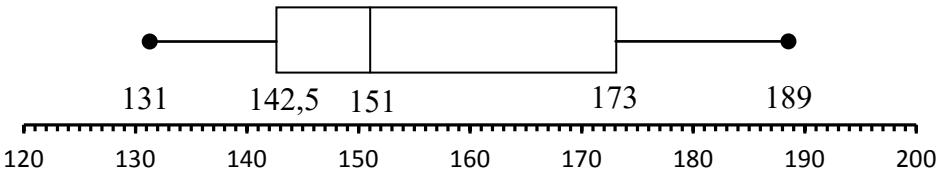
NOTE:

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed out version.
- Consistent accuracy applies in ALL aspects of the marking memorandum.
- Assuming answers/values in order to solve a problem is NOT acceptable.

NOTA:

- As 'n kandidaat 'n vraag TWEKEER beantwoord, merk slegs die EERSTE poging.
- As 'n kandidaat 'n poging om die vraag te beantwoord, doodgetrek het en nie dit oorgedoen het nie, merk die doodgetrekte poging.
- Volgehoue akkuraatheid word in ALLE aspekte van die nasienmemorandum toegepas.
- Aanvaarding van antwoorde/waardes om 'n probleem op te los, is ONaanvaarbaar.

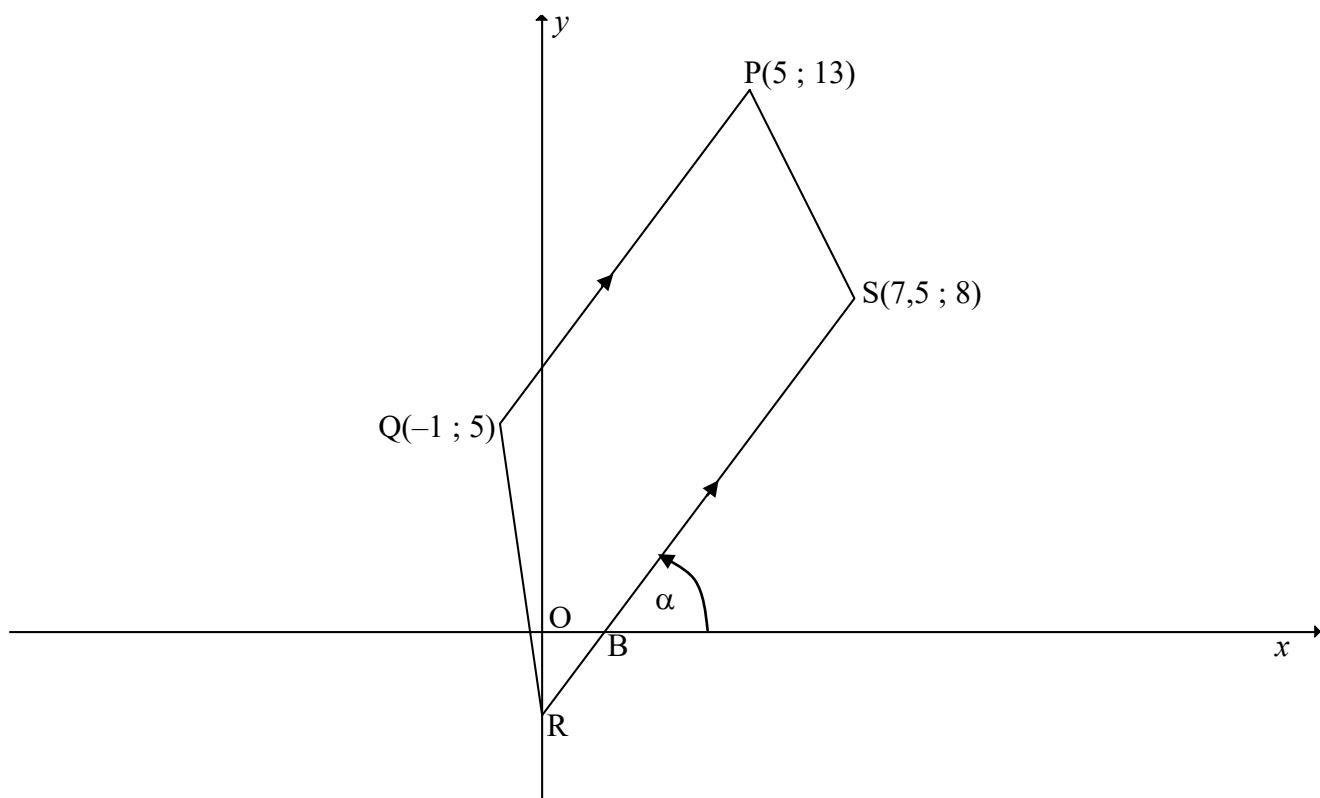
QUESTION/VRAAG 1

1.1	$\bar{x} = \frac{3310}{21}$ $= 157,62$	Answer only: Full marks slegs antw: volpunte	$\checkmark \frac{3310}{21}$ $\checkmark 157,62$ (2)
1.2	(131 ; 142,5 ; 151 ; 173 ; 189)		\checkmark 131 and/ en 189 \checkmark 142,5 \checkmark 173 \checkmark 151 (4)
1.3			\checkmark box/mond \checkmark whiskers/ snor (2)
1.4	positively skewed/positief skeef OR/OF skewed to the right/skeef na regs		\checkmark answer/ antwoord (1)
1.5	$\sigma = 17,27$		\checkmark \checkmark answer/ antwoord (2)
1.6.1	$\bar{x} = 157,62 + p$		\checkmark answer (1)
1.6.2	$\sigma = 17,27$		\checkmark answer/ antwoord (1) [13]

QUESTION/VRAAG 2

2.1	<p>As the temperature increases, the sales of ice-creams increase/<i>Soos die temperatuur styg, neem die verkope toe.</i></p> <p>OR/OF</p> <p>As the temperature decreases, the sales of ice-creams decrease/<i>Soos die temperatuur daal, neem die verkope af.</i></p>	<input checked="" type="checkbox"/> reason/rede (1)
2.2	The liveable temperature cannot keep on increasing/ <i>Die leefbare temperatuur kan nie aanhou styg nie.</i>	<input checked="" type="checkbox"/> reason/rede (1)
2.3	$a = -460,35$ $b = 30,09$ $\hat{y} = 30,09x - 460,35$ <p>OR/OF</p> $\hat{y} = -460,35 + 30,09x$ <div style="border: 1px solid black; padding: 5px; width: fit-content;"> <p>Answer only: Full marks <i>slegs antw: volpunte</i></p> </div>	<input checked="" type="checkbox"/> $-460,35$ <input checked="" type="checkbox"/> $30,09$ <input checked="" type="checkbox"/> equation/vgl (4)
2.4	$r = 0,96$	<input checked="" type="checkbox"/> 0,96 (1)
2.5	There is a <u>very strong</u> positive relationship (correlation)/ <i>Daar is 'n baie sterk positiewe verband (korrelasie).</i>	<input checked="" type="checkbox"/> very strong/baie sterk (1) [8]

QUESTION/VRAAG 3

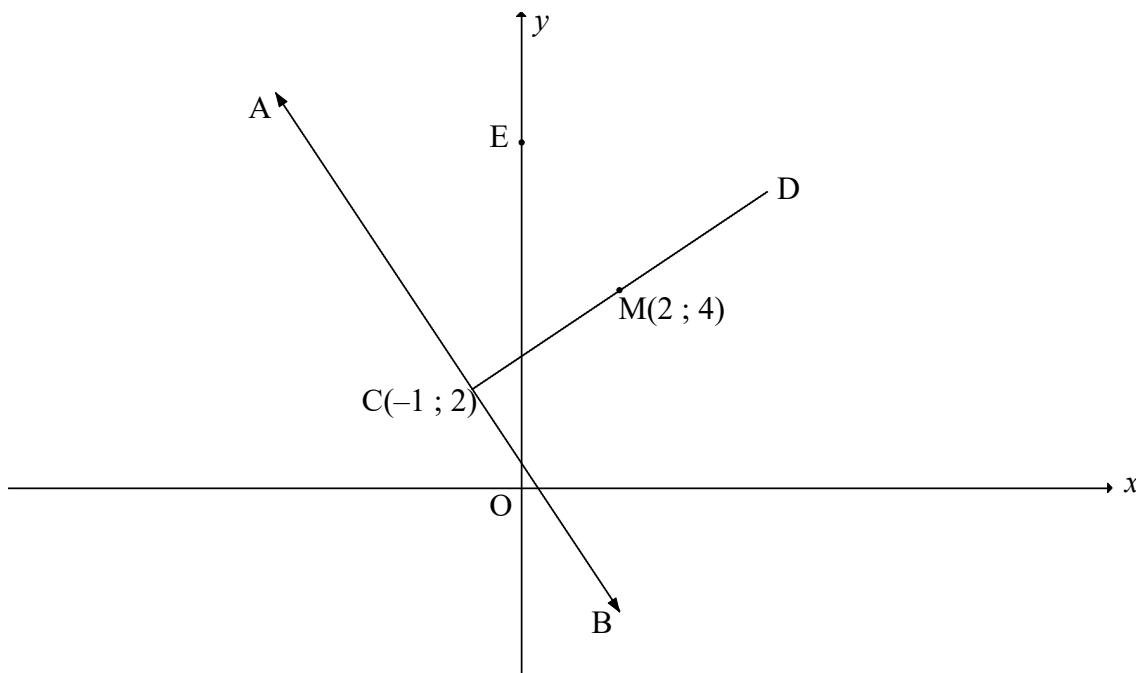


3.1	$\begin{aligned} PQ &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{(5 + 1)^2 + (13 - 5)^2} \\ &= 10 \end{aligned}$	<ul style="list-style-type: none"> ✓ use of distance formula/gebruik afstandformule ✓ correct subst into form/korrekte subst in formule ✓ 10 (3)
3.2	$\begin{aligned} m_{PQ} &= \frac{y_2 - y_1}{x_2 - x_1} \\ &= \frac{13 - 5}{5 - (-1)} \\ &= \frac{8}{6} = \frac{4}{3} \end{aligned}$ <div style="border: 1px solid black; padding: 5px; margin-left: 20px;"> Answer only: Full marks slegs antw: volpunte </div>	<ul style="list-style-type: none"> ✓ correct subst into gradient formula/korrekte subst in gradiëntformule ✓ gradient/gradiënt (2)

3.3	<p>Equation of line RS/Vgl van lyn RS:</p> $m_{RS} = m_{PQ} = \frac{4}{3} \quad (= \text{gradients, } \text{ lines} / = \text{gradiënte, } \text{ lyne})$ $y = mx + c$ $8 = \frac{4}{3} \left(\frac{15}{2} \right) + c$ $c = -2$ $y = \frac{4}{3}x - 2$ $\therefore 4x - 3y - 6 = 0$ <p style="text-align: center;">OR/OF</p> $y - y_1 = m(x - x_1)$ $y - 8 = \frac{4}{3} \left(x - \frac{15}{2} \right)$ $y = \frac{4}{3}x - 2$ $\therefore 4x - 3y - 6 = 0$	$\checkmark m_{RS} = \frac{4}{3}$ \checkmark subst of S(7,5 ; 8) and m into eq /subst van S(7,5 ; 8) en m in vgl \checkmark value of c /waarde van c or/of st form/st vorm \checkmark equation/vgl (4)
3.4	<p>B is the x-intercept of/is die x-afsnit van $y = \frac{4}{3}x - 2$</p> $0 = \frac{4}{3}x - 2$ $4x - 6 = 0$ $x = \frac{3}{2}$ <p style="text-align: center;">OR/OF</p> $4x - 3(0) - 6 = 0$ $4x - 6 = 0$ $x = \frac{3}{2}$	$\checkmark y = 0$ $\checkmark x = \frac{3}{2}$ (2)
3.5	$\tan \alpha = \frac{4}{3}$ $\alpha = 53,13^\circ = \hat{\text{OBR}}$ $\text{vert opp } \angle s/\text{rekoorste } \angle e$ $\hat{\text{ORB}} = 180^\circ - (90^\circ + 53,13^\circ)$ $= 36,87^\circ$	$\checkmark \tan \alpha = \frac{4}{3}$ $\checkmark 53,13^\circ$ $\checkmark 36,87^\circ$ (3)
3.6	$\begin{aligned} \text{BS} &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{\left(\frac{15}{2} - \frac{3}{2}\right)^2 + (8 - 0)^2} \\ &= 10 \\ \text{PQ} &\parallel \text{BS} \text{ and/en } \text{PQ} = \text{BS} \\ \text{PQBS} &= \text{parallelogram} \text{ (1 pair opp sides = and } \parallel \text{ / 1 pr tos sye = en } \parallel) \end{aligned}$ <p style="text-align: center;">OR/OF</p> <p>midpoint of/midpt van QS: $\left(\frac{-1+7.5}{2}; \frac{5+8}{2} \right) = \left(\frac{13}{4}; \frac{13}{2} \right)$</p> <p>midpoint of/midpt van PB: $\left(\frac{5+1.5}{2}; \frac{13+0}{2} \right) = \left(\frac{13}{4}; \frac{13}{2} \right)$</p> <p>PQBS = parallelogram (diags bisect each other/hoekl halv mekaar)</p> <p style="text-align: center;">OR/OF</p>	\checkmark correct subst into form/korrekte subst in formule $\checkmark \text{BS} = 10$ $\checkmark \text{BS} = \text{PQ}$ \checkmark reason/rede (4) $\checkmark \left(\frac{-1+7.5}{2}; \frac{5+8}{2} \right)$ $\checkmark \left(\frac{5+1.5}{2}; \frac{13+0}{2} \right)$ $\checkmark \left(\frac{13}{4}; \frac{13}{2} \right)$ \checkmark reason/rede (4)

$m_{QB} = \frac{5-0}{-1-1,5} = \frac{5}{-2,5} = -2$ $m_{PS} = \frac{13-8}{5-7,5} = \frac{5}{-2,5} = -2$ $m_{QB} = m_{PS}$ $\therefore QB \parallel PS$ $PQ \parallel BS$ PQBS = parallelogram (both pairs opp sides \parallel / beide pr tot sye \parallel)	$\checkmark m_{QB}$ $\checkmark m_{PS}$ $\checkmark QB \parallel PS$ \checkmark reason/rede (4)
OR/OF $BS = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ $= \sqrt{\left(\frac{15}{2} - \frac{3}{2}\right)^2 + (8-0)^2}$ $\therefore PQ = BS$ $= 10$ $QB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ $= \sqrt{(-1-1,5)^2 + (5-0)^2} = \sqrt{(2,5)^2 + (5)^2} = \frac{5\sqrt{5}}{2}$ or 5,59 $PS = \sqrt{(5-7,5)^2 + (13-8)^2} = \sqrt{(2,5)^2 + (5)^2} = \frac{\sqrt{125}}{2}$ or 5,59 $QB = PS$ PQBS = parallelogram (both pairs opp sides $=$ / beide pr tot sye $=$)	\checkmark correct subst into form/korrekte subst in formule \checkmark PQ = 10 \checkmark QB = PS \checkmark reason/rede (4) [18]

QUESTION/VRAAG 4



<p>4.1.1</p>	<p>Radius = $\sqrt{(2+1)^2 + (4-2)^2}$ $r = \sqrt{13}$ Equation of circle/vgl van sirkel: $(x-2)^2 + (y-4)^2 = 13$</p> <p style="text-align: center;">OR/OF</p> $(x-2)^2 + (y-4)^2 = r^2$ $(-1-2)^2 + (2-4)^2 = r^2$ $r^2 = 13$ $\therefore (x-2)^2 + (y-4)^2 = 13$	<p>✓ $\sqrt{(2+1)^2 + (4-2)^2}$ or/of $\sqrt{13}$ $\checkmark (x-2)^2 + (y-4)^2$ $\checkmark 13$</p> <p style="text-align: right;">(3)</p> <p>✓ $(x-2)^2 + (y-4)^2$ $\checkmark (-1-2)^2 + (2-4)^2$ $\checkmark 13$</p> <p style="text-align: right;">(3)</p>
<p>4.1.2</p>	<p>At/by D:</p> $\frac{-1+x_D}{2} = 2 \quad \frac{2+y_D}{2} = 4$ $-1+x_D = 4 \quad \text{and/en} \quad 2+y_D = 8$ $x_D = 5 \quad y_D = 6$ $D(5; 6)$ <p style="text-align: center;">OR/OF</p> <p>By inspection/deur inspeksie: D(5 ; 6)</p>	<p>✓ x - value/waarde \checkmark y - value/waarde</p> <p style="text-align: right;">(2)</p> <p>✓ x - value/waarde \checkmark y - value/waarde</p> <p style="text-align: right;">(2)</p>

4.1.3	$m_{MC} = \frac{4-2}{2+1} = \frac{2}{3}$ $m_{AB} \times m_{MC} = -1 \quad (\text{Tangent } \perp \text{ radius}/\text{raaklyn } \perp \text{ radius})$ $m_{AB} = -\frac{3}{2}$ $y - y_1 = m(x - x_1)$ OR/OF $y = mx + c$ $y - 2 = -\frac{3}{2}(x + 1)$ $2 = -\frac{3}{2}(-1) + c$ $y = -\frac{3}{2}x + \frac{1}{2}$ $y = -\frac{3}{2}x + \frac{1}{2}$	$\checkmark m_{MC} = \frac{4-2}{2+1} = \frac{2}{3}$ $\checkmark m_{AB} \times m_{MC} = -1$ $\checkmark m_{AB} = -\frac{3}{2}$ \checkmark subst m and $(-1 ; 2)$ into eq /subst m en $(-1 ; 2)$ in vgl \checkmark eq in standard form/ vgl in st vorm (5)
4.1.4	At/by E: $(0-2)^2 + (y-4)^2 = 13$ $(y-4)^2 = 9$ $y-4 = \pm 3$ $y = 7 \text{ or } y = 1$ E(0 ; 7) OR/OF At/by E: $(0-2)^2 + (y-4)^2 = 13$ $4 + y^2 - 8y + 16 = 13$ $y^2 - 8y + 7 = 0$ $(y-7)(y-1) = 0$ $y = 7 \text{ or } y = 1$ E(0 ; 7)	$\checkmark x = 0$ \checkmark simplification/ vereenvoudiging \checkmark y -values/waardes \checkmark E(0 ; 7) (4) $\checkmark x = 0$ \checkmark simplification/ vereenvoudiging \checkmark y -values/waardes \checkmark E(0 ; 7) (4)
4.1.5	$m_{EM} = \frac{y_2 - y_1}{x_2 - x_1}$ $= \frac{4-7}{2-0}$ $= -\frac{3}{2}$ $m_{AB} = -\frac{3}{2}$ $\therefore EM \parallel AB \quad (m_{EM} = m_{AB})$	$\checkmark m_{EM} = -\frac{3}{2}$ \checkmark reason/rede (2)

<p>4.2 The centres of the circles are / <i>Die middelpunte van die sirkels is</i> $P(-2 ; 4)$ and / <i>en</i> $Q(5 ; -1)$</p> $QP^2 = (-2 - 5)^2 + (4 - (-1))^2$ $QP = \sqrt{74} \approx 8,60 \text{ units}$ $\begin{aligned} r_M + r_p &= 5 + 3 \\ &= 8 \end{aligned}$ $\therefore r_M + r_p < QP$ <p><i>∴ The two circles do not intersect/Die twee sirkels sny nie</i></p>	<ul style="list-style-type: none"> ✓ both centres/<i>albei Midpte</i> ✓ QP ✓ correct subst into form/<i>korrekte subst in formule</i> ✓ distance between 2 centres/<i>afstand tussen 2 midpte</i> <p>✓✓ $r_M + r_p < QP$</p> <p style="text-align: right;">(6) [22]</p>
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QUESTION/VRAAG 5

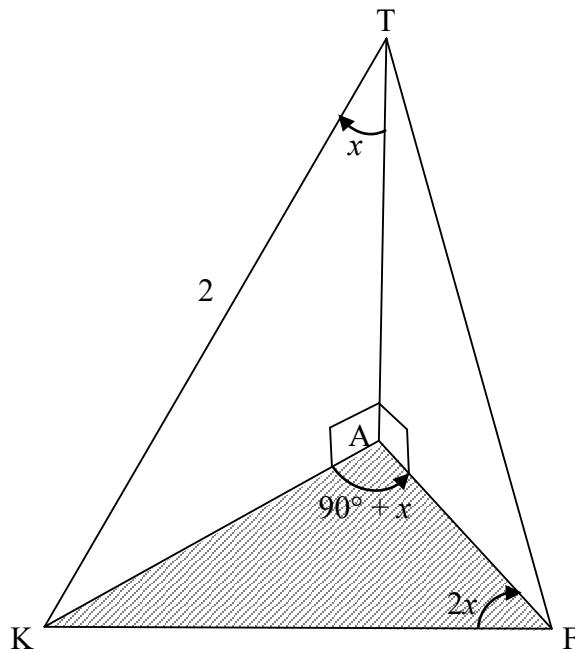
5.1	$ \begin{aligned} & x^2 + y^2 \\ &= (3 \sin \theta)^2 + (3 \cos \theta)^2 \\ &= 9 \sin^2 \theta + 9 \cos^2 \theta \\ &= 9(\sin^2 \theta + \cos^2 \theta) \\ &= 9(1) \\ &= 9 \end{aligned} $	<ul style="list-style-type: none"> ✓ simpl/vereenv ✓ CF/GF = 9 ✓ answer/antw (3)
5.2	$ \begin{aligned} & \sin(540^\circ - x) \cdot \sin(-x) - \cos(180^\circ - x) \cdot \sin(90^\circ + x) \\ & \sin(180^\circ - x) \cdot \sin(-x) - \cos(180^\circ - x) \cdot \sin(90^\circ + x) \\ &= (\sin x)(-\sin x) - (-\cos x)(\cos x) \\ &= -\sin^2 x + \cos^2 x \\ &= \cos 2x \end{aligned} $	<ul style="list-style-type: none"> ✓ $\sin(540^\circ - x) = \sin x$ ✓ $\sin(-x) = -\sin x$ ✓ $\cos(180^\circ - x) = -\cos x$ ✓ $\sin(90^\circ + x) = \cos x$ ✓ $-\sin^2 x + \cos^2 x$ ✓ $\cos 2x$ (6)
5.3.1	$ \begin{aligned} OT &= \sqrt{x^2 + p^2} \\ \sin \alpha &= \frac{y_T}{OT} \\ &= \frac{p}{\sqrt{x^2 + p^2}} \\ \frac{p}{\sqrt{x^2 + p^2}} &= \frac{p}{\sqrt{1+p^2}} \\ x^2 &= 1 \\ x &= -1 \end{aligned} $ <p style="text-align: center;">OR/OF (P lies in 3rd quadrant)</p> $ \begin{aligned} x^2 + y^2 &= r^2 \\ x^2 + p^2 &= (\sqrt{1+p^2})^2 \\ x^2 + p^2 &= 1 + p^2 \\ x^2 &= 1 \\ x &= -1 \end{aligned} $ <p style="text-align: center;">(P lies in 3rd quadrant)</p>	<ul style="list-style-type: none"> ✓ $OT = \sqrt{x^2 + p^2}$ ✓ $\sin \alpha = \frac{y_T}{OT}$ ✓ $x^2 = 1$ (3)
5.3.2	$ \begin{aligned} \cos(180^\circ + \alpha) \\ &= -\cos \alpha \\ &= -\left(\frac{-1}{\sqrt{1+p^2}}\right) \\ &= \frac{1}{\sqrt{1+p^2}} \end{aligned} $	<ul style="list-style-type: none"> ✓ $x^2 + y^2 = r^2$ ✓ subst ✓ $x^2 = 1$ (3)
		<ul style="list-style-type: none"> ✓ $-\cos \alpha$ ✓ answer/antw (2)

<p>5.3.3</p> $\begin{aligned} \cos 2\alpha &= \cos^2 \alpha - \sin^2 \alpha \\ &= \left(\frac{-1}{\sqrt{1+p^2}} \right)^2 - \left(\frac{p}{\sqrt{1+p^2}} \right)^2 \\ &= \frac{1}{1+p^2} - \frac{p^2}{1+p^2} \\ &= \frac{1-p^2}{1+p^2} \end{aligned}$	<p>✓ expansion/ uitbreiding</p> <p>✓✓ squaring each term/kwadreer elke term</p> <p>(3)</p>
<p>OR/OF</p> $\begin{aligned} \cos 2\alpha &= 1 - 2 \sin^2 \alpha \\ &= 1 - 2 \left(\frac{p}{\sqrt{1+p^2}} \right)^2 \\ &= 1 - 2 \left(\frac{p^2}{1+p^2} \right) \\ &= 1 - \frac{2p^2}{1+p^2} \\ &= \frac{1+p^2 - 2p^2}{1+p^2} \\ &= \frac{1-p^2}{1+p^2} \end{aligned}$	<p>✓ expansion/ uitbreiding</p> <p>✓ squaring/kwadrering</p> <p>✓ writing as single fraction/skryf as enkelterm</p> <p>(3)</p>
<p>OR/OF</p> $\begin{aligned} \cos 2\alpha &= 2 \cos^2 \alpha - 1 \\ &= 2 \left(\frac{-1}{\sqrt{1+p^2}} \right)^2 - 1 \\ &= 2 \left(\frac{1}{1+p^2} \right) - 1 \\ &= \frac{2}{1+p^2} - 1 \\ &= \frac{2-1-p^2}{1+p^2} \\ &= \frac{1-p^2}{1+p^2} \end{aligned}$	<p>✓ expansion/ uitbreiding</p> <p>✓ squaring/kwadrering</p> <p>✓ writing as single fraction/skryf as enkelterm</p> <p>(3)</p>

5.4.1	<p>The identity is undefined for/<i>die identiteit is ongedefinieerd as:</i> $2\sin^2 x = 0$ $\therefore \sin x = 0: x = 0^\circ; 180^\circ$ or/of $\tan x = \infty: x = 90^\circ$ $\therefore x = 0^\circ; 90^\circ; 180^\circ$</p>	<p>✓ $x = 0^\circ$ ✓ $x = 90^\circ$ ✓ $x = 180^\circ$</p> <p>(3)</p>
5.4.2	<p>LHS/LK = $\frac{2 \tan x - \sin 2x}{2 \sin^2 x}$ $= \frac{2 \left(\frac{\sin x}{\cos x} \right) - 2 \sin x \cos x}{2 \sin^2 x}$ $= \left(\frac{2 \sin x - 2 \sin x \cos^2 x}{\cos x} \right) \times \frac{1}{2 \sin^2 x}$ $= \frac{2 \sin x (1 - \cos^2 x)}{\cos x} \times \frac{1}{2 \sin^2 x}$ $= \frac{2 \sin x (\sin^2 x)}{\cos x} \times \frac{1}{2 \sin^2 x}$ $= \frac{\sin x}{\cos x}$ $= \tan x$ $= \text{RHS/RK}$</p> <p style="text-align: center;">OR/OF</p> $\text{LHS/LK} = \frac{2 \tan x - \sin 2x}{2 \sin^2 x}$ $= \frac{2 \left(\frac{\sin x}{\cos x} \right) - 2 \sin x \cos x}{2 \sin^2 x} \times \frac{\cos x}{\cos x}$ $= \frac{2 \sin x - 2 \sin x \cos^2 x}{2 \sin^2 x \cos x}$ $= \frac{2 \sin x (1 - \cos^2 x)}{2 \sin^2 x \cos x}$ $= \frac{2 \sin x \cdot \sin^2 x}{2 \sin^2 x \cos x}$ $= \frac{\sin x}{\cos x}$ $= \tan x$ $= \text{RHS/RK}$	<p>✓ $\frac{\sin x}{\cos x}$ ✓ $2 \sin x \cdot \cos x$</p> <p>✓ simplify numerator/<i>vereenv teller</i></p> <p>✓ factorising/<i>fakt</i></p> <p>✓ $1 - \cos^2 x = \sin^2 x$</p> <p>✓ simplify to/<i>vereenv na</i> $\frac{\sin x}{\cos x}$</p> <p>(6)</p>
		<p>✓ $\frac{\sin x}{\cos x}$ ✓ $2 \sin x \cdot \cos x$</p> <p>✓ simpl/<i>vereenv</i></p> <p>✓ factorising/<i>fakt</i></p> <p>✓ $1 - \cos^2 x = \sin^2 x$</p> <p>✓ simplify to /<i>vereenv na</i> $\frac{\sin x}{\cos x}$</p> <p>(6)</p> <p>[26]</p>

QUESTION/VRAAG 6

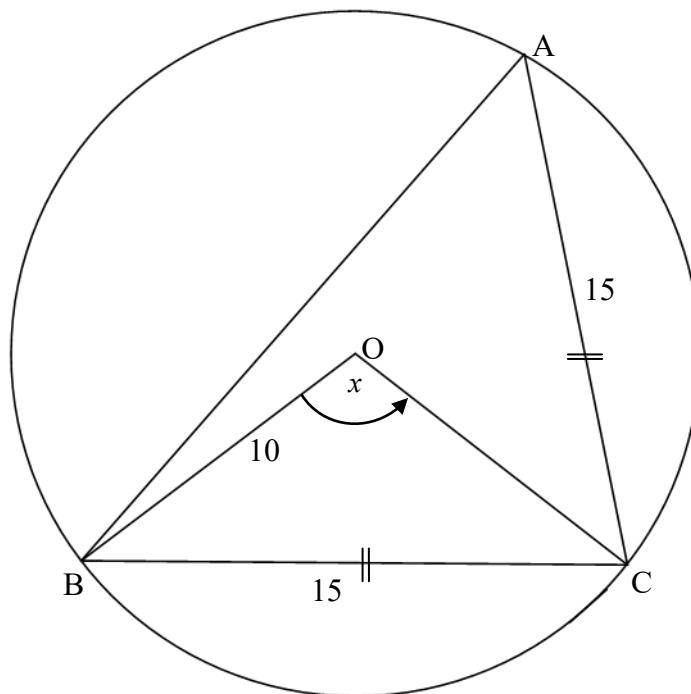
6.1



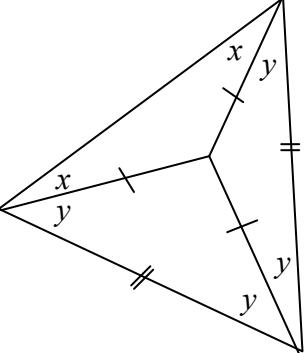
<p>6.1.1 In ΔTAK:</p> $\frac{AK}{KT} = \sin K\hat{T}A$ $AK = KT \cdot \sin x$ $= 2 \sin x$ <p style="text-align: center;">OR/OF</p> $\frac{\sin K\hat{T}A}{AK} = \frac{\sin K\hat{T}}{KT}$ $\frac{\sin 90^\circ}{2} = \frac{\sin x}{AK}$ $AK = 2 \sin x$	<ul style="list-style-type: none"> ✓ correct trig ratio/ korrekte trigverh. ✓ answer/antw (2) <ul style="list-style-type: none"> ✓ correct subst into sine rule/korrekte subst in sin-reël ✓ answer/antw (2)
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6.1.2	<p>In ΔAKF:</p> $\frac{KF}{\sin K\hat{A}F} = \frac{AK}{\sin A\hat{F}K}$ $\frac{KF}{\sin(90^\circ + x)} = \frac{AK}{\sin 2x}$ $KF = \frac{AK \cdot \sin(90^\circ + x)}{\sin 2x}$ $= \frac{2 \sin x \cdot \cos x}{2 \sin x \cdot \cos x}$ $= 1$ <p style="text-align: center;">OR/OF</p> <p>In ΔAKF:</p> $\frac{KF}{\sin K\hat{A}F} = \frac{AK}{\sin A\hat{F}K}$ $\frac{KF}{\sin(90^\circ + x)} = \frac{AK}{\sin 2x}$ $KF = \frac{AK \cdot \sin(90^\circ + x)}{\sin 2x}$ $= \frac{AT \cdot \tan x \cdot \cos x}{2 \sin x \cdot \cos x}$ $= \frac{2 \cos x \cdot \frac{\sin x}{\cos x} \cdot \cos x}{2 \sin x \cdot \cos x}$ $= 1$ <div style="border: 1px solid black; padding: 10px; margin-left: 20px;"> $\cos x = \frac{AT}{2}$ $\therefore AT = 2 \cos x$ </div>	<ul style="list-style-type: none"> ✓ using sine rule/ gebruik sin-reël ✓ correct subst into sine rule/korrekte subst in sin-reël ✓ $\sin(90^\circ + x) = \cos x$ ✓ $2 \sin x \cdot \cos x$ ✓ 1 <p style="text-align: right;">(5)</p> <ul style="list-style-type: none"> ✓ using sine rule/ gebruik sin-reël ✓ correct subst into sine rule/korrekte subst in sin-reël ✓ $\sin(90^\circ + x) = \cos x$ ✓ $2 \sin x \cdot \cos x$ ✓ 1 <p style="text-align: right;">(5)</p>
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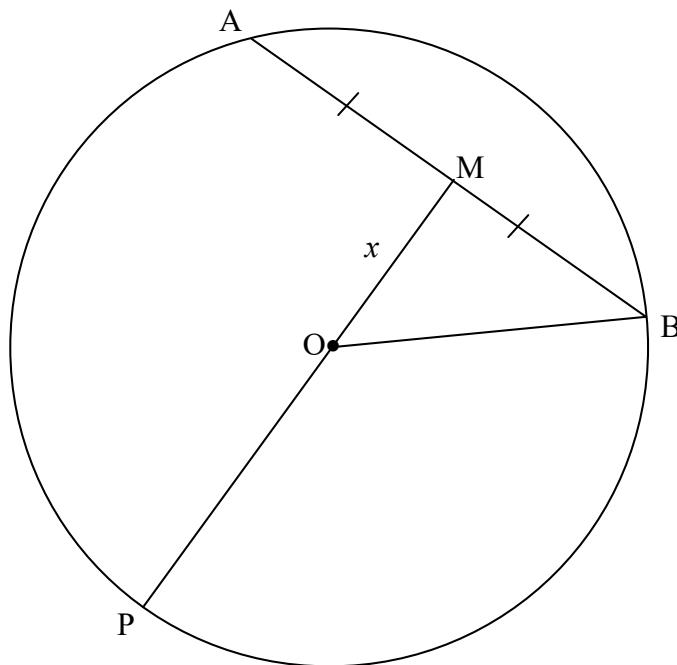
6.2



<p>6.2.1 In ΔBOC:</p> $BC^2 = BO^2 + CO^2 - 2 \cdot BO \cdot CO \cdot \cos x$ $15^2 = 10^2 + 10^2 - 2(10)(10) \cdot \cos x$ $200 \cos x = -25$ $\cos x = -0,125$ $x = 180^\circ - 82,82^\circ$ $= 97,18^\circ$	<ul style="list-style-type: none"> ✓ using cosine rule/ gebruik cos-reël ✓ correct subst/ korrekte subst ✓ $\cos x = -0,125$ ✓ $97,18^\circ$ <p>OR/OF</p>
<p>Draw a line $OD \perp BC$:</p> $BD = DC \quad (\text{line from centre } \perp \text{ on chord})$ $\Delta OBD \cong \Delta OCD \quad (90^\circ; h; s)$ $\sin \frac{x}{2} = \frac{7,5}{10}$ $\frac{x}{2} = 48,59^\circ$ $\therefore x = 97,18^\circ$	<ul style="list-style-type: none"> ✓ S/R ✓ correct ratio/ korrekte verh ✓ value of/waarde <i>van</i> $\frac{x}{2}$ ✓ $97,18^\circ$

6.2.2	$\hat{BAC} = 48,59^\circ \quad (\angle \text{ at centre} = 2 \times \angle \text{ at circ}/\angle \text{ by midpt} = 2 \times \angle \text{ omt})$ $\hat{ABC} = \hat{BAC} = 48,59^\circ \quad (\angle \text{'s opp equal sides}/\angle e \text{ teenoor} = \text{sye})$ $\therefore \hat{ACB} = 82,82^\circ \quad (\text{sum of } \angle \text{s of } \Delta/\text{som van } \angle \text{e van } \Delta)$ <p style="text-align: center;">OR/OF</p> $\begin{aligned} \hat{ACB} &= \frac{1}{2} \hat{AOB} && (\angle \text{ at centre} = 2 \times \angle \text{ at circle}) \\ &= \frac{1}{2} [360^\circ - 2(97,18^\circ)] \\ &= 82,82^\circ \end{aligned}$ <p style="text-align: center;">OR/OF</p> $\begin{aligned} \hat{OCB} &= \frac{1}{2} (180^\circ - 97,18^\circ) && (\angle \text{'s opp equal sides}; \text{sum of } \angle \text{s of } \Delta) \\ &= 41,41^\circ && (\angle e \text{ teenoor} = \text{sye}; \text{som van } \angle \text{e van } \Delta) \end{aligned}$  $\begin{aligned} \hat{ACB} &= 2(41,41^\circ) \\ &= 82,82^\circ \end{aligned}$	$\checkmark S$ $\checkmark S$ $\checkmark 82,82^\circ$ (3) $\checkmark S$ $\checkmark S$ $\checkmark 82,82^\circ$ (3) $\checkmark S$ $\checkmark S$ $\checkmark 82,82^\circ$ (3)
6.2.3	Area/Oppervlakte ΔABC $= \frac{1}{2} (BC)(AC) \sin \hat{ACB}$ $= \frac{1}{2} (15)(15)(\sin 82,82^\circ)$ $= 111,62 \text{ cm}^2$	\checkmark correct subst into area rule/korrekte subst in opp-reël $\checkmark 111,62 \text{ cm}^2$ (2) [16]

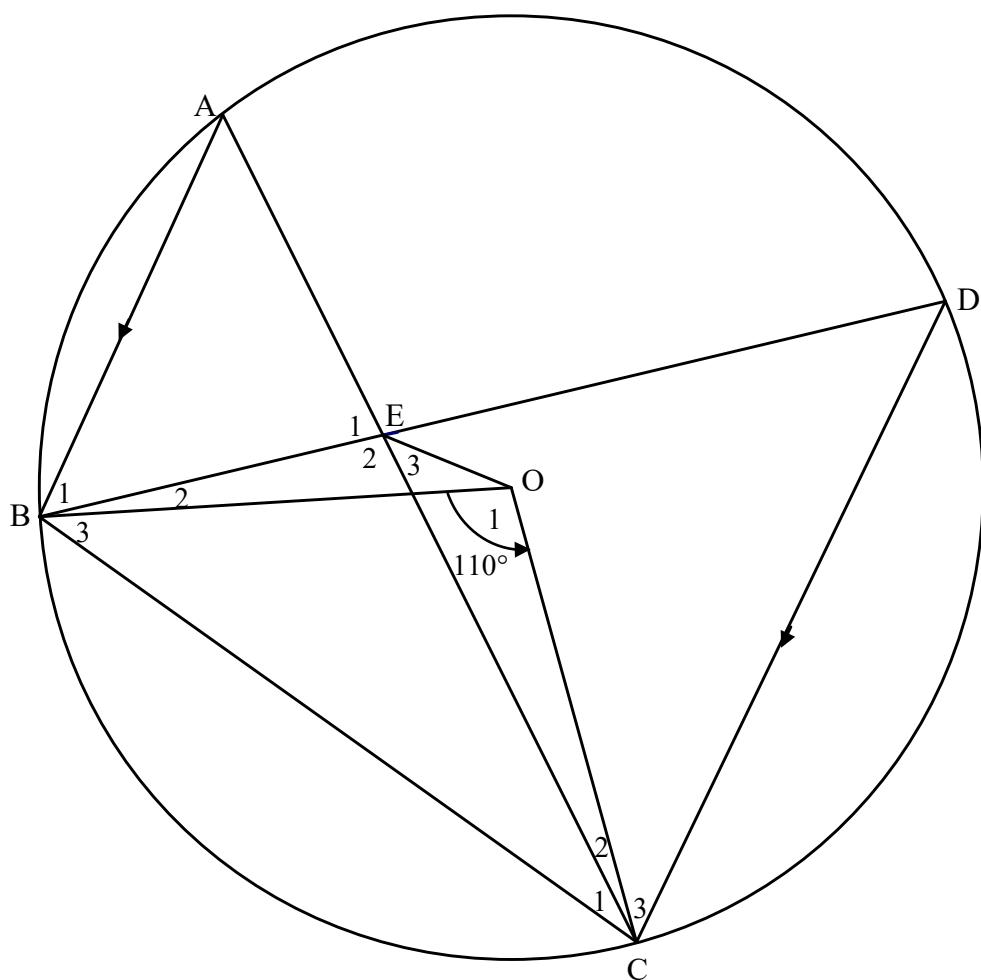
QUESTION/VRAAG 7



7.1	MB = 10 cm	✓ answer/antw (1)
7.2	line from centre to midpoint of chord is perpendicular to chord/lyn vanaf midpt na midpt van koord is loodreg op koord OR/OF line from centre bisects chord/lyn vanaf midpt halveer koord	✓ answer/antw (1) ✓ answer/antw (1)
7.3	$\frac{MP}{OM} = \frac{5}{2}$ $\frac{x + OP}{x} = \frac{5}{2}$ $2x + 2OP = 5x$ $OP = \frac{3x}{2}$ OR/OF $\frac{OP}{OM} = \frac{3}{2}$ $OP = \frac{3x}{2}$	$\checkmark \frac{x + OP}{x} = \frac{5}{2}$ $\checkmark OP = \frac{3x}{2}$ $\checkmark \frac{OP}{OM} = \frac{3}{2}$ $\checkmark OP = \frac{3x}{2}$ (2)

7.4	$\text{OM}^2 + \text{MB}^2 = \text{OB}^2$ $x^2 + 10^2 = \left(\frac{3x}{2}\right)^2$ $4x^2 + 400 = 9x^2$ $5x^2 = 400$ $x^2 = 80$ $x = 8,94 \text{ or } 4\sqrt{5} \text{ or } \sqrt{80}$	<ul style="list-style-type: none"> ✓ subst into/subst Pythagoras ✓ $4x^2 + 400 = 9x^2$ ✓ answer/antw (3) <p>[7]</p>
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QUESTION/VRAAG 8

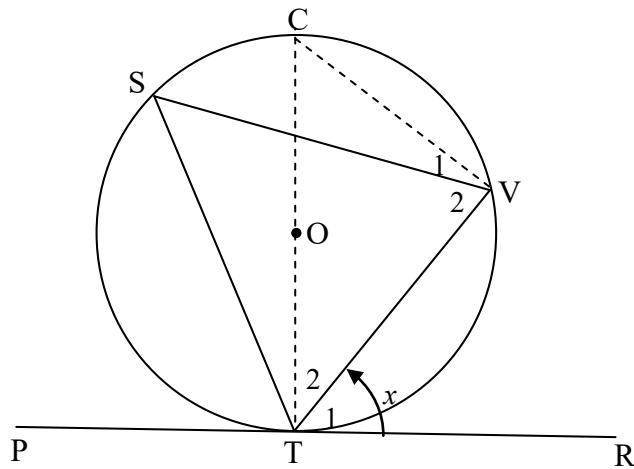


8.1.1	$\hat{D} = \frac{1}{2} \hat{O}_1 = 55^\circ$ (\angle at centre = $2 \times \angle$ at circ / \angle by midpt = $2 \times \angle$ by omt)	$\checkmark S \checkmark R$ (2)
8.1.2	$\hat{A} = \frac{1}{2} \hat{O}_1 = 55^\circ$ (\angle at centre = $2 \times \angle$ at circ / \angle by midpt = $2 \times \angle$ by omt)	$\checkmark S \checkmark R$ (2)
OR/OF		
	$\hat{A} = \hat{D} = 55^\circ$ (\angle s in same segment / \angle e in dieselfde segment)	$\checkmark S \checkmark R$ (2)
8.1.3	$\hat{B}_1 = \hat{D} = 55^\circ$ (alternate \angle s / verwiss \angle e; $AB \parallel DC$) $\hat{E}_2 = \hat{B}_1 + \hat{A}$ (ext \angle of Δ = sum of opp \angle s / buite \angle v Δ = som v tos \angle e) $= 55^\circ + 55^\circ$ $\hat{E}_2 = 110^\circ$	$\checkmark S \checkmark R$ $\checkmark R$ \checkmark answer/antw (4)
8.2	$\hat{E}_2 = \hat{O}_1 = 110^\circ$ (proven in/bewys in 8.1.3) BEOC is a cyclic quadrilateral (equal \angle s subtended by line / gelyke \angle e onderspan deur lyn)	$\checkmark S$ $\checkmark R$ (2) [10]

QUESTION/VRAAG 9

9.1	the interior opposite angle/die teenoorstaande binnehoek.	✓ answer/antw (1)
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9.2

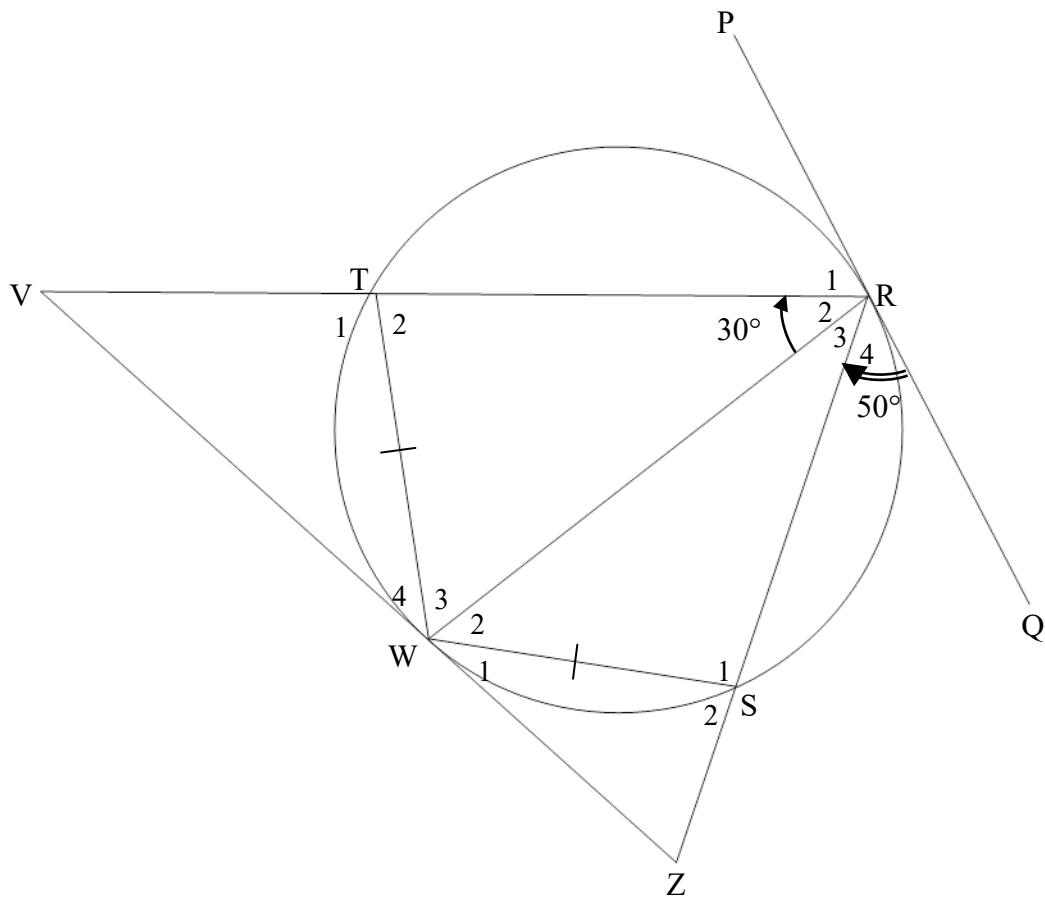


Construction: Draw diameter CT and join CV.

Konstruksie: Trek middellyn CT en verbind CV.

$\hat{V}_1 + \hat{V}_2 = 90^\circ$	\angle in semi-circle/ \angle in halfsirkel	✓ S ✓ R
$\hat{T}_2 = 90^\circ - x$	Tangent \perp diameter/radius/raaklyn \perp middellyn/radius	✓ R
$\therefore \hat{C} = x$	Sum of the angles of triangle/Som van die hoeke van 'n driehoek	✓ S
$\therefore \hat{S} = x$	\angle 's same segment/ \angle e in dieselfde segment	✓ R
$\therefore \hat{VTR} = \hat{S}$		(5)

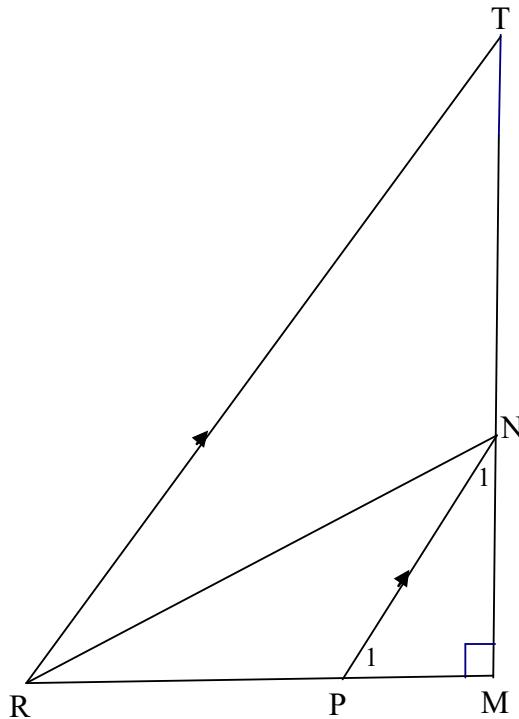
9.3



9.3.1	Equal chords subtend equal \angle s/Gelyke koorde onderspan gelyke \angle e	\checkmark R (1)
9.3.2	$\hat{W}_4 = 30^\circ$ (tan chord theorem/rkl-koordst) $\hat{W}_1 = 30^\circ$	\checkmark answer/antw \checkmark reason/rede \checkmark answer/antw (3)
9.3.3(a)	$\hat{R}_4 = \hat{W}_2 = 50^\circ$ (tan chord theorem/rkl-koordst) $\hat{S}_2 = \hat{R}_3 + \hat{W}_2$ (ext \angle of Δ /buite \angle v Δ) $\therefore \hat{S}_2 = 80^\circ$	\checkmark S \checkmark R \checkmark S (3)
	OR/OF	
	$\hat{R}_2 = \hat{R}_3 = 30^\circ$ (= chords subtend $=\angle$ s / = kde onderspan= \angle e) $\hat{R}_4 = \hat{W}_2 = 50^\circ$ (tan chord theorem/rkl-koordst) $\therefore \hat{S}_2 = 80^\circ$	\checkmark S \checkmark R \checkmark S (3)

9.3.3(b)	$\hat{T}_2 = \hat{S}_2 = 80^\circ$ (ext \angle of cyclic quad/buite \angle van koordevh) $V + \hat{W}_4 = \hat{T}_2$ (ext \angle of Δ /buite \angle van Δ) $\therefore \hat{V} = 50^\circ$	✓ S ✓ R ✓ S ✓ S (4)
9.3.4	In ΔRVW and/en ΔRWS : $\hat{R}_2 = \hat{R}_3 = 30^\circ$ (proven/bewys in 9.3.1) $\hat{V} = \hat{W}_2 = 50^\circ$ (proven/bewys in 9.3.3) $V\hat{W}R = \hat{S}_1$ (3rd \angle in Δ) $\therefore \Delta RVW \parallel\parallel \Delta RWS$ ($\angle\angle\angle$) $\therefore \frac{WR}{RV} = \frac{RS}{WR}$ ($\Delta RVW \parallel\parallel \Delta RWS$) $\therefore WR^2 = RV \cdot RS$	✓ using the correct Δ s/ gebruik korrekte Δ e ✓ S ✓ S ✓ R (3rd \angle in Δ) or ($\angle\angle\angle$) ✓ S (5) [22]

QUESTION/VRAAG 10



10.1.1	corresponding \angle s/ooreenkomsige \angle e; $PN \parallel RT$	✓ answer/antw (1)
10.1.2	\angle ; \angle ; \angle OR/OF \angle ; \angle	✓ answer/antw (1)
10.2	$\frac{PM}{RM} = \frac{PN}{RT} \quad (\Delta PNM \parallel\!\!\!\parallel \Delta RTM)$ $= \frac{PN}{3PN}$ $= \frac{1}{3}$	✓ S ✓ S (2)
10.3	$\frac{PM}{RM} = \frac{1}{3} \quad \therefore \frac{RP}{RM} = \frac{2}{3}$ $RN^2 - PN^2 = (RM^2 + NM^2) - (PM^2 + NM^2) \quad (\text{Pyth})$ $= RM^2 - PM^2$ $= \left(\frac{3}{2}RP\right)^2 - \left(\frac{1}{2}RP\right)^2$ $= \frac{9}{4}RP^2 - \frac{1}{4}RP^2$ $= 2RP^2$	✓ Use of Pyth. for RN^2 and PN^2 ✓ $RM = \frac{3}{2}RP$ ✓ $PM = \frac{1}{2}RP$ ✓ $\frac{9}{4}RP^2$ & $\frac{1}{4}RP^2$ (4)

OR/OF

	$ \begin{aligned} RN^2 - PN^2 &= (RM^2 + NM^2) - (PM^2 + NM^2) \quad (\text{Pyth}) \\ &= RM^2 - PM^2 \\ &= (3PM)^2 - PM^2 \\ &= 8PM^2 \\ &= 2(2PM)^2 \\ &= 2RP^2 \end{aligned} $ <p style="text-align: center;">OR/OF</p> $ \begin{aligned} RN^2 - PN^2 &= (RM^2 + NM^2) - (PM^2 + NM^2) \quad (\text{Pyth}) \\ &= RM^2 - PM^2 \\ &= (RP + PM)^2 - PM^2 \\ &= RP^2 + 2RP \cdot PM + PM^2 - PM^2 \\ &= RP^2 + 2RP \cdot \frac{1}{2} RP \\ &= 2RP^2 \end{aligned} $	<ul style="list-style-type: none"> ✓ Use of Pyth. for RN^2 and PN^2 ✓ $RM = RP + PM$ ✓ expansion/ <i>uitbreiding</i> ✓ $PM = \frac{1}{2} RP$ <p style="text-align: right;">(4) [8]</p>
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TOTAL/TOTAAL: **150**